Optimal Monetary Policy with Output and Asset Price Volatility in an Open Economy: Evidence from Kenya

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Abstract

This paper attempts to establish optimal response of monetary policy to output, inflation and asset price volatility in a small open economy, taking into account optimisation behaviour of households and firms. The empirical analysis suggest that monetary policy responds to deviation of interest rate and output growth rate from their targets with greater weight compared to asset prices and inflation. The analysis also show that commitment to a monetary policy rule achieves output and inflation objectives as well as a higher level of welfare compared to discretionary monetary policy rule.

JEL Classifications: E3, E32, G1

Keywords: Optimal monetary policy, Asset price volatility, Output volatility

1 Introduction

Monetary authority in developing economies desire to hasten the rate of economic growth and maintain price stability simultaneously. Interest rate is employed to regulate prices, which in turn influence level of utilisation of economy’s resources and the size of output gap. However, maintaining price stability may open a large recessionary gap due to high interest rate (Woodford, 2003; Divino, 2009). In addition, distortions in the balance sheets of firms and households occur as a result of asset price misalignment from their fundamental value during and after periods of price stability (Schwartz, 1995; Borio & Lowe, 2002). Notwithstanding sub-optimal debt accumulation by households and firms as a result of asset price misalignment, lenders may predispose themselves to losses by lending against distorted balance sheets\(^1\). This not only impedes capital formation, but also increases fragility of the financial sector, which affects output stability. Hence, maintaining price stability without considering changes in asset price changes may undermine achieving output growth target.

A small open economy is exposed to external shocks that affect nominal exchange rate stability\(^2\); Clarida et al. (2001); Corsetti & Pesenti (2005); Divino (2009); Fujiwara & Wang (2017). The movements in the nominal exchange rate induce instability in domestic prices and output, hence

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\(^1\) Stiglitz & Weiss (1981) Lenders do not have full information about the quality of the borrowers of investible funds and the viability of investment projects to be financed by the funds borrowed. Therefore, lenders require collateral or borrowers signal their quality by providing assets that can be sold to recover the funds borrowed should the borrower default.

\(^2\) Bernanke & Gertler (2000); Mishkin (2001) distortions in the balance sheets as a result of Asset prices misalignment, on the one hand, borrowers may either borrow too to be sufficient for capital formation required to achieve the target growth rate or too much against their asset, which may precipitate liquidity distress. On the other hand, lenders are predisposed to default risk

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require a monetary policy intervention by changing interest rates. Yet, the change in interest rates may, first, be inconsistent with the output gap and inflation stabilisation target level. Secondly, interest rate differential between the domestic and the foreign financial markets as a result of monetary policy response to inflation and asset price instability cause portfolio flows that again trigger exchange rate movement.

Furthermore, with output and inflation stability targets, interest rate changes, for instance, to accelerate output growth rate to achieve target growth rate requires low interest rate, but this causes nominal exchange rate depreciation and inflation. This generates a trade-off between achieving output growth rate and inflation targets in an economy with a strong exchange rate pass-through. In this case, monetary policy intervention in the foreign exchange market, induces distortions in prices that drives output away from potential output (Clarida et al., 2001; Corsetti & Pesenti, 2005). Hence, whereas price stabilisation efforts may either drive other set of prices and output from the respectively targets, unregulated prices achieve undesirable level of output and prices.

Therefore, the main objective of this paper is to analyse optimal response of monetary policy to output, inflation and asset price volatility in Kenya. To this end, the paper develops a social welfare function, from the general equilibrium model. Then the social welfare function is solved numerically using the dynamic programming method of Bellman & Lee (1984), taking into account optimisation decisions of households and firms. An approach that has been emphasized and used by Rotemberg & Woodford (1997), Benigno (2004) and Divino (2009) in their analysis of optimal monetary policy. The formulation and numerical solution of the social welfare problem as dynamic program enables estimation of the time path of monetary policy rate that maximises social welfare. The weights estimated indicate optimal response of monetary policy to deviations of objective variables from their target, considering the static and dynamic responses of agents to monetary policy actions in an economy. This enables the evaluation of monetary policy outcome under discretion and consistency rules.

The parameter estimates of the social welfare function indicate that monetary authority should respond with greater weight to deviation of output from the target compared to deviation of asset prices and inflation from their respective targets in order to maximise welfare. With respect to optimal rules, dynamic programming results indicate that commitment to a monetary policy rule leads to higher welfare than discretion. The findings are corroborated by regression estimates of the quadratic loss function. The results suggest that, as much as output, asset price and inflation stabilisation are important; output stability has the greatest influence on welfare and hence should be prioritised among the monetary policy stabilisation objectives. The finding are consistent with Woodford (2003) and Divino (2009) analyses of optimal monetary policy.

There is dearth of literature on the optimal response of monetary policy to output and inflation stability, for example (Clarida et al., 2001; Woodford, 2003; Benigno, 2004). However, few studies have analysed optimal response of monetary policy to inflation and output stability in an open economy while taking into account asset price instability. Yet, besides the reaction of monetary policy to output and price instability, optimality of a monetary policy response is equally important, as it determines not only output growth and welfare, but also effectiveness of monetary policy.

Moreover, the interest rate changes as a result of monetary policy actions to address asset price and output fluctuations cause exchange rate movements, which affects inflation. This paper attempts to fill this gap by analysing the optimal response of monetary policy to output, inflation and asset price instability in a small open economy. This approach provides a more comprehensive analysis of the monetary policy stabilisation problem faced by monetary authorities in small open developing economies. In this regard, this paper is related to Rotemberg & Woodford (1997), Benigno (2004) and Divino (2009) with respect to the analysis of optimal response of monetary policy to output, interest rate and exchange rate instability respectively.
The main innovations in this paper are, first, it includes equity and bond prices in establishing weights with which monetary authority should respond to deviation of variables of interest from their desired level. This approach allows the analysis of differences in monetary policy response to equity and bond price instability given that they respond differently to changes in interest rates. Secondly, the social welfare criterion for evaluating optimal monetary response is solved numerically using dynamic programming method of Bellman & Lee (1984). The optimal solution yields an estimate of optimal penalty imposed on the deviation of variables from their targets, social welfare and the optimal time path of policy rate. This enables the evaluation of welfare outcomes of monetary policy intervention in an open economy under discretionary and consistent rules.

This paper focuses on Kenya because, first it is a small open economy susceptible to strong exchange rate pass through to domestic prices and output, due to a managed floating exchange rate regime. Secondly the Nairobi Securities Exchange is dominated by firms in the financial sector, which not only bear the initial impact of monetary policy stimuli, but also transmit monetary policy shocks to the real sector. In this regard, Kenya offers a good case for analysing optimality of monetary policy in a small open developing economy, taking into account stabilisation of asset prices. In addition, the active trading of bonds and equities of firms in the financial sector as well as the proximity of the firms to the monetary policy stimuli, enables a better analysis of the optimal response of monetary policy to the asset prices movements.

The rest of the paper is organised as follows. The next section briefly describes evaluation of monetary policy and how it is used to stabilise output, inflation and asset prices. Section 3 explains optimal monetary policy intervention in the economy. Sections 4 and 5 discusses the methodology, data and main results respectively, while section 6 summarises issues from the main results. The section concludes that a consistent monetary policy rule not only achieves price and output stability objectives, but also attains a higher welfare compared to a discretionary monetary policy rule.

2 Response of monetary policy to inflation, output and asset price instability in Kenya

Monetary policy in Kenya, like other developing countries, is implemented to primarily achieve price stability, which is essential for encouraging investment and output growth. Besides, price stability, monetary policy is also employed to mitigate output fluctuations. The evolution of monetary policy in Kenya has been shaped by economic challenges that required economic reforms to hasten the rate of economic growth. Notably, liberalisation and removal of price controls between 1985 and early 1990s, necessitated priorisation of price stability over output growth in the implementation of monetary policy. This is because, liberalisation and price decontrols led to increase in inflation, which undermined output growth. The emphasis on price stability objective achieved low and stable inflation rate, but at the expense of slow output growth rate by the end of 1990 and early 2000, whereby Kenya had the lowest average growth rate of 2.1 percent compared to 4.1 percent and 3.9 percent between 1980-1989 and 2000-2009 respectively (figure 1).
The monetary policy framework in Kenya started with money targeting whereby monetary authorities changed money supply in tandem with growth in nominal output. This ensures that liquidity is just enough to finance transactions in the economy (McCallum, 1999). However, in an economy riddled with structural rigidities as well as exclusion of a substantial proportion of economic agents from the banking system, changes in the stock of money has a small impact on the agents' money holding relative to a change in interest rate. As a result, money targeting framework may be ineffective in controlling liquidity in all segment of the economy, and hence, inflation (Moore, 1988; Mishkin, 2004).

In view of the ineffectiveness of money targeting framework in controlling inflation, monetary authority in Kenya like in other developed and developing countries are transitioning to inflation targeting. Monetary policy in transition to inflation targeting regimes prioritises inflation and output objectives. Monetary policy operations utilise market based instruments to achieve inflation and output targets. There is also higher transparency and rationalisation of a monetary policy decision than in money targeting framework, to inform expectations of the public regarding expected interest rate and inflation. The public in turn changes actual and expected interest rate in the direction suggested by monetary policy (Mishkin, 2004). This increases effectiveness of monetary policy against fluctuation in output and inflation in economies with low monetary policy pass through to the economy like Kenya (Monacelli, 2003; Misati et al., 2011). In deed figure 1 indicates that, broad money and market lending rate move counter-cyclically to output growth rate, implying that monetary policy can be used to stabilise output and inflation simultaneously, despite existence of structural rigidities in the economy (Federico et al., 2014; Were, 2014).

Kenya is a small open economy, with a managed floating exchange rate regime. This allows a pass through of foreign prices to domestic prices especially through prices of imported inputs and exports. In addition, foreign capital flows through the Nairobi Securities Exchange fluctuated between 50 per cent in 2010 to a low of 4 per cent, as a proportion of stock market turn over, for the year 2011-2014 (CMA, 2010, 2014, 2015). Hence, volatility in foreign capital turnover may induce significant changes in exchange rate, equity and bond prices. Movements in exchange rate and deviations of asset prices from the discounted value of asset returns undermine stability of the financial sector and output, especially when the shares turnover of companies in financial sector constitute over 70 percent of the overall NSE turn over. Yet monetary policy mainly focuses on
output and inflation stability when adjusting monetary policy rate (Were, 2014).
Moreover, gradual adjustment of monetary policy instruments to stabilise inflation, output and exchange rate precludes asset price stabilisation. The advantage of gradually adjusting monetary policy rate towards the target is that it creates inertia in the change in actual and expected market interest rates in the direction of the policy rate. This reduces uncertainty in the financial market, which is essential for investment and stability in asset prices. However, the change in the policy rate may not be optimal in so far as the monetary policy response function excludes information as well as expectations of the public regarding asset prices. Therefore, there is need to shed some light on the monetary response to inflation, output and asset price stability as well as optimality of the monetary policy stabilisation actions.

3 Optimal monetary policy stabilization of output and Prices

The views on optimal monetary policy start from the perspective that an economy can achieve an efficient level of inflation, output and employment, if there are no distortions in wages and prices. The resultant level of inflation and output maximises individual and social welfare. Such an outcome cannot be improved upon without prejudice to welfare of other agents in the society, and hence a monetary intervention only leads to inefficient outcome with a lower level of welfare. This is the so-called “best equilibrium”. The implication of the best equilibrium outcome is that monetary policy interventions in the economy can lead to prices that distort incentives to work, save and invest. As a result, output growth rate may not only be insufficient to maximise welfare, but also cause instability prices. Therefore, so long as the equilibrium results from economic agents facing the right prices, a monetary policy intervention in the economy is not required (Rotemberg & Woodford, 1997; Svensson, 1997).

However, distortions in the economy caused by shocks, market power of agents on the demand, and supply side and information asymmetry among agents during transactions establish distorted price. Price distortions either misallocate or lead to under-utilisation of an economy’s resources. This results to actual output and inflation deviating from potential output and inflation target respectively. Even if there are no price distortions, such that established prices lead to efficient utilisation of resources and hence efficient output level, the resultant inflation and output may be undesirable from the society’s point of view (Svensson, 1997; Benigno, 2004). Consequently, monetary policy intervention is required to remove the price distortions, which leads to the so-called “first best equilibrium”. In particular, monetary authority can alter prices by either changing liquidity or policy interest rate, to influence agents’ behaviour, so that agents can adjust their saving, investment and consumption as well as expectation such that a socially desirable inflation and output level is attained. This is relevant for market economies since they are not devoid of current and future commodity and financial asset price distortions. For instance, labour unions, market power, changes in demand for goods, services and capital as well as natural factors, influence domestic prices. In addition, developing economies have levels of national outputs that are lower than the socially desirable level. Hence, there is need for monetary policy intervention to accelerate output to potential output and to the level that is socially desirable.

Even though Svensson (1997) and Benigno (2004) imply that monetary policy intervention in prices and level of output is required to either remove distortion or achieve social welfare objective, they do not take into account the instability that may result from policy intervention. The instability emanates from the fact that commitment to a monetary policy rule, which yields second best equilibrium after removing distortion, does not take into account agents’ expectations and optimisation decisions. In addition, the rules that guide intervention, may not incorporate new information that is relevant for intervention to improve outcome of a consistent monetary policy.
action (Kydland & Prescott, 1977). As a result, a consistent monetary policy yields welfare level that is suboptimal compared to the first equilibrium when a price distortion is removed (King, 1997; Kydland & Prescott, 1977; Svensson, 1997).

Nevertheless, discretionary policy overcomes weakness in commitment, by taking into account optimisation decisions of the agents, when intervening to address distortions each time. This affords monetary authority flexibility to respond to unanticipated price and output changes as well as dynamic optimisation behavior of economic agents, thereby achieving an optimal policy intervention. Indeed, this is relevant for the financial markets in which investors make decisions frequently to optimise their portfolio holding. In addition, small open developing economies like Kenya are susceptible to unpredictable capital flows and terms of trade changes, which affect asset and commodity prices respectively. Hence, there is need for monetary authority to apply discretionary monetary policy rule to address price stability which also affect output stability.

Yet, discretion results in, first, higher volatility in either prices or output. This is because, discretion does not provide agents with rules and information that they can use to make current optimisation decision. Consequently, as a result of inconsistency of a discretionary monetary policy intervention, agents adjust their decision as they get information, which affects stability of prices and output. Indeed, inconsistency in monetary policy action is a major cause of volatility in forward looking markets as it increases uncertainty (Svensson, 1997; McCallum, 1999; Woodford, 2003). Secondly, discretion allows monetary authority to use its superior information compared to the public, with respect to changes in the monetary policy instrument, to pursue its main objective with ease at the expense of other objectives perceived important by the public. This is the case where the public cannot observe and verify actual changes in liquidity caused by actions of the Central Bank. King (1997) argues that monetary policy under discretion does not consider inflation expectations of the public when responding to output shocks. As a result, stabilising output by changing liquidity increases instability in expected inflation as well as actual inflation. In this case, even though monetary policy manages to stabilise output, it does not effectively stabilise inflation. Consequently, discretion results to a lower welfare compared to commitment.

In spite of the inconsistency of a discretionary monetary policy intervention that makes it fourth best equilibrium policy intervention\(^2\), Rogoff (1985) asserts that discretionary intervention can be improved by appointing an agent whose social preferences are the same as those of the society. In particular, a more conservative agent with respect to output and inflation stabilisation, than the society employs his/her discretion to achieve price and output stability. However, the agent’s conservative intervention may yield price and output level that is less desirable from the society’s perspective. Rogoff (1985) and King (1997) establish that a conservative agent is favours when the society prefers more growth compared to price stability. However, the social preference as depicted by social welfare function, may require intermediate combination of growth and price stability, that is a combination of positive growth and non-zero average inflation rate. In particular, in Kenya, as it is in other developing countries where income growth objective is important, a positive inflation rate is required to encourage saving and investment by making nominal interest rate positive. Hence, a conservative agent achieves an allocation that is inferior to an agent commited to a particular monetary policy rule when stabilising output and inflation, but superior to pure discretion.

Nonetheless, the society can do better with an agent who has built a credible reputation of embodying social preference when intervening in the economy. An agent with such reputation acts with discretion to maximise individual welfare. Since, the preferences of the agent and public are the same, the outcome of the agent’s intervention satisfies social preferences. Consequently, social

\(^2\)Barro & Gordon 1983; King 1997; Svensson 1997 government intervention in the market by removing distortion results in the first best equilibrium; intervention with a commitment rule leads to a second best allocation; discretion with a conservative agent achieves an allocation that is third best; while discretion leads to fourth best equilibrium
welfare is maximised. This implies that, on the one hand, the agents' choice of price level and corresponding output are consistent with social expectation and preferences. On the other hand, a reputable agent provides credible information to the public, relevant for making current decisions. More importantly, the public has a rule to follow when making optimisation decisions. Therefore, a reputable agent achieves output and price stability objective that is similar to commitment (Rogoff, 1985; Lockwood et al., 1998). One main weakness of reputation under discretionary monetary policy intervention is that the agent may not be effective in responding to unforeseen price distortions that the agent has no reputation of dealing with. For example, a Central Bank which has a reputation of maintaining price stability, cannot credibly address shocks that destabilise output, exchange rate and asset prices.

Empirical analysis of optimality of monetary policy intervention in the economy evaluates social welfare outcomes of monetary policy under commitment and discretion in general. The analyses focus on the approaches that achieve price stability, because when prices are stabilised at a level that enables a socially acceptable allocation and production, they lead to maximisation of social welfare. Therefore, optimality of monetary policy can be assessed with respect to the monetary policy rule that stabilise actual and expected inflation. For example Rogoff (1985), Rotemberg & Woodford (1997), Svensson (1997) and King (1997) analyse the effectiveness of commitment and discretion in maintaining inflation stability. The studies establish that commitment to an interest rate rule, when responding to high inflation, leads to inflation stability, although output growth rate deviates from the target. The interest rate rule also leads to higher instability in output despite inflation and interest rate being stable. Woodford (2003) focuses on a consistent interest rate adjustment by monetary authority in response to inflation changes. In this analysis, smooth adjustment of interest rate in the expected direction informs the expectation of the public, who optimise based on the information available. The study establishes that interest rate adjustment with inertia has a higher welfare compared to surprise adjustment. The inertial adjustment of interest rate provides information required for formation of expectation about future asset price, which reduce uncertainty in forward looking markets.

Divino (2009), Clarida et al. (2001), Corsetti & Pesenti (2005) and Benigno (2004) extend the analysis to include exchange rate. In this way, consider distortions in the domestic prices emanating from foreign economies. Their analytical solution of the social welfare function establishes that a consistent interest rate adjustment to stabilise inflation leads to output instability, because changes in interest rate, affects exchange rate, which then causes a deviation of output from the socially desirable level. In this case, inflation stabilisation efforts by the monetary policy causes exchange rate distortions which reallocates resources, resulting in an equilibrium that is socially undesirable. There are few limitations to these analyses. Firstly, though consistent with second best equilibrium, they do not take into account financial asset prices, like bond and equity prices when monetary policy is responding to price distortions. As long as equity and bond prices, which result from optimisation decision of agents on the financial market are not taken into account, a discretionary intervention cannot do better than a commitment rule. More importantly, asset price movements affect aggregate demand by changing the net-worth and wealth of firms and households. Fluctuations in aggregate demand as a result of asset price change induce instability in output. Furthermore, asset price instability stifle growth by undermining the integrity of the financial sector to mobilise and distribute capital in the economy by distorting return on capital and balance sheets. Therefore, monetary authority eager to stabilise output and enhance growth, especially in developing economies, has to include asset prices in its objective function. Secondly, equity and bond prices are a source of information that can be used by monetary authority to...
stabilise inflation (Bernanke & Gertler, 2000; Mishkin, 2001). Finally, in the general analytical solutions of Divino (2009), Clarida et al. (2001), Corsetti & Pesenti (2005) and Benigno (2004), social optimisation problem with monetary policy intervention do not yield numerical results that are easy to compare.

Therefore, this paper tries to overcome these weaknesses by analysing optimal monetary policy response to output and asset price volatility. A welfare analysis approach is used, because optimal intervention is more effectively evaluated by comparing welfare outcomes of alternative interventions. In addition, the welfare optimisation approach takes into account the optimisation decision of the public, which is relevant for monetary policy. The social problem is also solved using dynamic programming numerical method, which allows a quantitative comparison.

4 Methodology and Data

The monetary policy actions influence relative prices to achieve inflation and output stabilisation objectives. Underpinning price and output changes towards the monetary policy target is the portfolio adjustment by optimising agents. Households optimise their portfolio holding to maximise utility, while firms adjust price Calvo (1983) style to maximise profits. With respect to households, movements in inflation and asset prices as a result of monetary policy change liquidity services of money balances held by the public. Besides, liquidity services, inflation and asset prices affect the amount of wealth and disposable income and hence, consumption of goods and services. Since holding assets is risky and an average household is risk averse, a constant relative risk aversion utility function suffice in describing utility derived from consuming goods and services as well as holding financial assets. Hence utility function of a representative household is given by:

$$V_t = E_t \sum_{i=0}^{\infty} \beta^i \left[ C_t^{1-\sigma} \frac{1}{1-\sigma} - \frac{N_t^{1+\gamma}}{1+\gamma} + \frac{(M_t/P_t)^{1-\eta}}{1-\eta} \right]$$

(1)

Where consumption $C_t$ real money $M_t/P_t$, labour $N_t$ and $\beta$ discount rate. Parameters $\sigma$ coefficient of relative risk aversion with respect to consumption, $\gamma$ inverse of the Frisch labour supply elasticity, $\eta$ coefficient of relative risk aversion with respect to money balances. Household optimisation decision determine optimal $C_t$, $M_t$ and $N_t$. Using the household and firm optimisation decisions output is given by:

$$y_t = E_t y_{t+1} - \frac{\beta}{\sigma} \left[ i_{bt} - E_t (\bar{\epsilon}_{t+1} + \pi_{t+1}) \right]$$

(2)

Where $i_{bt}$ interest rate, $y_t$ output, $\bar{\epsilon}_{t+1}$ expected change in exchange rate and $\pi_{t+1}$ is the expected inflation rate obtained from rearranging the Philip’s curve 3 below.

$$\pi_t = \frac{(1-\Theta)(1-\Theta\beta)}{(\Theta)} mc_t + \beta E_t (\pi_{t+1})$$

(3)

$mc_t$ is the marginal cost. The price setting decisions of firms to maximises discounted profits establish the Philip’s curve. The derivations for output and the Phillips curve functions are given in appendix I.

From the output function and the Phillips curve, the exchange rate influences output via two channels. The first channel is through changes in output as a result of change in domestic demand. In addition, exchange rate movements alter balance sheets of firms and households, which not only affects credit worthiness, but also wealth, and hence, aggregate demand (Mishkin, 2001; Divino, 2009). The second channel is through change in marginal cost of producing goods and services. Small open economies with flexible exchange rate regime, exchange rate movement have a significant effect on domestic marginal costs as it influences real wage and cost of intermediate imported goods. Interest rate $i_{bt}$, affect yield on bonds as well as return on investment, and hence
equity prices. In this case changes in interest rates influence aggregate demand by affecting asset prices.

Making interest rate $i_{bt}$ the subject using aggregate supply function yields a monetary policy response function given by:

$$i_{bt} = \frac{\sigma}{\beta} (E_t y_t + 1 - y_t) + \frac{1}{\sigma} [\beta E_t (\bar{\varepsilon}_{t+1} + \pi_{t+1})]$$  \hspace{1cm} (4)

Therefore, the Central Bank can achieve output and inflation objectives by changing the policy rate taking into account, output gap, expected exchange rate depreciation and inflation. The changes in interest rate according to equation 4 minimises $\text{mc}_t$, inflation, exchange rate and output gap deviations from zero (Woodford, 2003; Gali & Monacelli, 2005).

However, a change in monetary policy rate according to equation 4 may not be optimal from the society’s perspective, because it does not take into account social preferences about inflation and output as well as the reaction of the public to the monetary policy decision. Optimal monetary policy achieves a price level that allows the agents to optimise their consumption, leisure and financial asset holding, according to the social preferences as depicted by a social welfare function. A good approximation of the social welfare function is the second order Taylor approximation of the household utility function Rotemberg & Woodford (1997). Divino (2009) and Woodford (2003) use a similar approach. The use of money in the utility function equation 1 to approximate social loss function captures the effect of monetary policy on social welfare, as a result of changes in money balance and asset prices. Even though a separable utility function with respect to consumption and leisure can be used as in Woodford (2003), money in the utility function with leisure is more appropriate, because it is broader. In this regard, a second order Taylor approximation around the steady state of the money in the utility function is used to approximate the social welfare function. This is the quadratic loss function given by equation 5 below. The details of derivation of the quadratic loss function are provided for in appendix II

$$L_t = \sum_{t=0}^{\infty} \beta^t \left( \gamma \pi_t^2 + \gamma y_t^2 + \gamma Q_t^2 + \gamma B_t^2 \right)$$  \hspace{1cm} (5)

$$y_t = \tilde{y} + x_t + b((1 + i) - \pi_{t+1}) + e_t$$  \hspace{1cm} (6)

$$\pi_t = ((1 + i) - \pi_{t+1}) + C x_t$$  \hspace{1cm} (7)

$$Q_t = \frac{(Q_{t+1} + \pi_t \varepsilon_t)}{1 + i}$$  \hspace{1cm} (8)

$$B_t = \frac{B_{t-1}}{1 + i}$$  \hspace{1cm} (9)

Where $L_t$ is the social loss to be minimised, $\gamma_{\pi}$, $\gamma_{y}$, $\gamma_{Q}$, $\gamma_{B}$ are contributions of inflation, income, equity price and debt instability to social loss respectively. $\tilde{B}_t$ is the debt level, $y_t$ income, $\pi_t$ inflation, $Q_t$ equity price, $\tilde{y}$ potential income, $\beta$ discount factor, $\varepsilon_t$ nominal exchange rate, $x_t$ is the public deficit, $C$ contribution of public deficits to inflation and $t$ is time. Indeed equation 5 depicts preferences of the public with respect to inflation, output, equity and bond prices, which also affect consumption, leisure, and money balances. An optimal monetary policy action is results to price, interest rate, bond and equity prices, that minimise equation 5, subject to the first order condition of the utility maximisation problem of the public given by equations 6 to 9. Equation 6 is the Lucas aggregate supply function; 7 describes change in inflation overtime; equations 8 and 9 are the equity price and debt stock equations, respectively obtained from the household optimisation decision. This specification takes into account the fact that monetary policy cannot fully influence rational expectations of the public. This affects their optimisation decisions in relation to monetary policy actions. Following Lucas & Stokey (1983), monetary authority in this case choose a policy rate that enables an allocation of credit that maximises social welfare given the resource constraint and the decisions of agents in the economy.
In particular, a monetary authority chooses a target interest rate level and decides on the time path the policy interest rate should follow to stabilise inflation. The time path of the monetary policy rate then influences the time path of the market interest rate. Therefore, an optimal monetary policy intervention requires the path of monetary policy rate to minimise the social welfare function over the entire path. Thus, the solution provided by the monetary authority to the social optimisation problem depends on the monetary policy rule it adopts, when responding to instability in the variables in the social welfare function.

A commitment policy rule entails solving optimisation problem once and for all, and then the monetary authority applies the same optimal rule to maximise social welfare overtime. In particular, the monetary authority commits to an interest rate rule to minimise social welfare function. Thus, the problem can be recast as a dynamic optimisation problem, whereby \( L_t \) is a state variable and monetary policy interest rate is the decision or policy variable. Therefore, under commitment, the Central Bank commits credibly to a particular rule, when intervening in the market to stabilise price such that \( L_t \) is the lowest. However, under discretion, equation 5 is solved subject to the private sector's optimisation without commitment to a policy rule. This specification allows the application of dynamic programming method of Bellman & Lee (1984) to solve for the optimal interest rate path. The same approach has been used by Woodford (2003), though Söderlind (1999) argues that optimal response can be estimated using regression methods. The reduced form of equation 4 is proximal to equation 5. However, regression estimates of the quadratic loss function parameters are average weights that do not reflect optimisation behaviour of the Central Bank and the public as well as reaction of agents, to policy decision (Rotemberg & Woodford, 1997). The next section presents estimates of the social welfare function weights.

The estimates are based on data for Kenya between first quarter of 2000 and fourth quarter of 2016. Output, interest rate, nominal exchange rate, repo rate, equity and bond prices are passed through Hodrick Prescott filter to obtain the trend and cycle. The output trend approximates potential output, while the long term trend in bond prices is consistent with the yield curve. With respect to inflation, monetary authority in Kenya have an inflation target of 5 percent, with an allowance of 2.5 percentage point deviation from the target. Therefore, inflation stabilisation entails keeping inflation within the range 5 ±2.5 percent. Data on equity and bond prices is obtained from the NSE, while output, interest and rate exchange rate is obtained from the Central Bank of Kenya.

5 Main Results

Table 1 presents the least square estimates of the reduced form of 4, with repo rate as the monetary policy rate. The parameters on the loss function indicate the weight monetary authority attach to the variable when changing monetary policy to maximise the society’s welfare. Thus, the coefficient of the estimated quadratic loss function is the penalty monetary policy imposes on the deviation of the variable in the social welfare function from the target or its long run level.
### Table 1: Quadratic Loss function

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<td>Output gap</td>
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<td>-0.037**</td>
<td>-0.017**</td>
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<td>(0.100)</td>
<td>(0.011)</td>
<td>(0.008)</td>
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<tr>
<td>Output growth rate</td>
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<td>-0.080*</td>
<td>-0.167*</td>
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<td>(0.162)</td>
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<td>(0.011)</td>
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<td>Exchange rate</td>
<td>0.320***</td>
<td>0.312*</td>
<td>0.156*</td>
<td>0.138*</td>
<td>0.121*</td>
<td>0.165*</td>
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<td>Equity prices</td>
<td>-0.018</td>
<td>-0.012</td>
<td>-0.015*</td>
<td>-0.012*</td>
<td>-0.004*</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.011)</td>
<td>(0.009)</td>
<td>(0.001)</td>
<td>(0.001)</td>
<td>(0.001)</td>
<td></td>
</tr>
<tr>
<td>Inflation</td>
<td>0.019</td>
<td>0.019</td>
<td>0.009</td>
<td>0.006</td>
<td>0.028*</td>
<td>0.011</td>
</tr>
<tr>
<td></td>
<td>(0.033)</td>
<td>(0.032)</td>
<td>(0.008)</td>
<td>(0.005)</td>
<td>(0.002)</td>
<td>(0.012)</td>
</tr>
<tr>
<td>Bond prices</td>
<td>0.031***</td>
<td>0.025</td>
<td>0.040*</td>
<td>0.003</td>
<td>0.007***</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.017)</td>
<td>(0.016)</td>
<td>(0.004)</td>
<td>(0.006)</td>
<td>(0.004)</td>
<td></td>
</tr>
<tr>
<td>interest rate</td>
<td>0.371*</td>
<td>0.369*</td>
<td>0.312*</td>
<td>0.356*</td>
<td>0.383*</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.029)</td>
<td>(0.028)</td>
<td>(0.019)</td>
<td>(0.021)</td>
<td>(0.028)</td>
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<tr>
<td>constant</td>
<td>1.329</td>
<td>1.420</td>
<td>2.080*</td>
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<tr>
<td></td>
<td>(1.206)</td>
<td>(1.165)</td>
<td>(0.100)</td>
<td>(0.130)</td>
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<tr>
<td>Volatility</td>
<td>0.005*</td>
<td></td>
<td></td>
<td>0.717*</td>
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<tr>
<td></td>
<td>(0.001)</td>
<td></td>
<td></td>
<td>(0.078)</td>
<td></td>
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<tr>
<td>R-squared</td>
<td>0.662</td>
<td>0.655</td>
<td></td>
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</table>

**Notes:** In this regression the dependent variable is the deviation of repo rate from its trend, Output gap is the deviation of actual output from the potential output (the trend). Explanatory variables in the quadratic loss function are in deviation form. Standard errors are in (). * 1%, ** 5% and *** 10%.

The regression estimates are valid given that endogeneity test in Table 3 in appendix II indicates that there is no endogenous relationship between the dependent and independent variables in the model. In column 1 of table 1, the social welfare loss function is estimated with output gap. The first regression uses squared deviation of output from the potential level. The coefficient on output gap indicates that if output deviates from potential output by one unit increase, the policy rate reduces by 0.073 per cent, but the reduction in the policy rate is statistically insignificant. However, monetary authority responds to a 1 per cent deviation of exchange rate by imposing a penalty of 0.32 per cent. With respect to stock market, on the one hand, the Central Bank increases the policy rate by 0.031 per cent statistically significantly when bond price deviate by 1 per cent. On the other hand, the Central Bank does not respond to deviations of equity prices from the long term trend. This indicates that the Central Bank, in its effort to maximise social welfare, does not give significant weight to deviation of output and equity prices from their potential levels. A possible explanation is that developing economies have abundant resources like labour and natural resources that are grossly underutilised. As a result, they have a high potential output as well a large output gap. The monetary policy efforts to increase resource employment by increasing aggregate demand causes inflation. This is due to the presence of structural rigidities, that impede responsiveness of supply of goods and services and hence demand for factors of production to monetary stimuli. In this case, an expansionary monetary policy causes excess demand and inflation.
rather than increasing aggregate supply. Consequently, monetary authorities find it optimal to focus on inflation stabilisation, which can be more effective in controlling than closing the output gap.

However, this is counter intuitive to the overall objective of monetary policy in developing economies, which is that the level of output is given the highest priority as indicated by the higher positive level at which inflation is stabilised compared to developed economies. The higher average level of inflation stabilisation implies that money growth rate is higher and real interest rate is lower in developing countries compared to developed countries, to stimulate output growth rate.

Developing economies like that of Kenya require a higher rate of economic growth to improve incomes and social welfare. Besides, a higher output growth rate increases the speed with which the output gap is closed. In this regard, monetary authorities change policy interest rate with the intention of achieving a higher and steady rate of growth in national income. Hence, in table 1 column two, quadratic loss function is reestimated with national income growth rate instead of actual national income gap to clarify the results in column 1 of table 1. The coefficient on income growth rate is negative and statistically insignificant as well as of almost the same size as that of actual income gap reported in column 1. Even though the results indicate that monetary authorities do not respond significantly to deviations in output as well as output growth rate from the output long trend and growth rate target, respectively, this may be due to misspecification of the model, because estimated model does not take into account variation of volatility overtime.

On the one hand, monetary authorities consider volatility in output and asset prices, because it affects commodity prices and returns on investment, which in turn influence output stability (Stulz, 1986; Lester et al., 2012). On the other hand, an average household is risk averse and therefore, risk as measured by volatility, enters its welfare function explicitly as the variance. Thus, the social welfare function maximised by monetary authority to optimise social welfare is misspecified if volatility is omitted from the estimated equation.

Therefore, to overcome omitted variable bias in the social welfare parameter estimation, time varying volatility is included as an explanatory variable in the quadratic loss function in columns 3 to 5 of table 1. The parameter estimates in column 4 and 5 indicate that monetary authority respond to volatility by increasing policy rate, since the Autoregressive Conditional Heteroscedasticity (ARCH) and Generalised Autoregressive Conditional Heteroscedasticity (GARCH) terms are positive and statistically significant. The volatility in the welfare function is positive and significant as well as the largest in the parameter estimates with output growth rate. This indicates that monetary authorities accord the greatest weight in responding to volatility in the social welfare function. A possible explanation of the response is that volatility, which is a measure of uncertainty and risk in the financial market as well as the entire economy, affects prices, consumption and investment decisions. Consequently, it affects welfare adversely especially for risk averse agents. As a result, monetary authority act strongly against volatility to mitigate its adverse effects.

With respect to output deviation from the long term trend and output growth rate deviation from the target growth, monetary authorities reduce the policy rate statistically significantly. The weight of its response is about 0.017 and 0.08 respectively. The weight monetary authority employs in responding to output deviation suggests that monetary policy is not only a counter-cyclical, but also expansionary. The response can be explained by the need to accelerate as well as stabilise output growth, which is one of the main objectives of monetary policy in developing economies. Higher economic growth improves income per capita as well as disposable income of people in an economy which they use to spend on goods and service. Besides higher disposable income as a result of higher income growth rate, the income fluctuation smoothing monetary policy reduces fluctuations in households’ income, which increases welfare.

Even after controlling for volatility, the exchange rate coefficient is positive and statistically signif-
In column 5 of table 1, the Central Bank imposes a penalty of 0.21 per cent when exchange rate deviates from the desired path by 1 per cent. In a small open economy like that of Kenya, exchange rate movements affect aggregate demand first, by changing domestic prices relative to foreign prices, thereby switching demand between foreign and domestic produced goods. Secondly, exchange rate affect producer and consumer price indices, which monetary policy seeks to control. Hence, the response of monetary authorities to exchange rate changes. Finally, arbitrage in the international financial market increase sensitivity of exchange rate to interest rate differential between domestic and foreign markets. Furthermore, exchange rate movements affect returns on foreign denominated asset that influence portfolio investment and wealth of investors as well as consumption and welfare of agent. Therefore, exchange rate movement not only affects portfolio decision of private agents, but also expectations about future wealth. This is a possible explanation for the significant response of monetary policy against exchange rate deviations from the desired path. The result is consistent with Divino's (2009) analysis of optimal monetary policy in a small open economy.

The Central Bank responds to deviations in the domestic money market interest rates with a weight 0.356 per cent for a 1 per cent deviation from the long run level. The Central Bank intervenes in a credit money economy by changing the interest rate that it lends to commercial banks, which in turn influences market interest rate, exchange rate, inflation, yield on bonds and equity prices. In this regard, monetary authorities can achieve stability in asset prices and output by influencing market interest. In addition, money market interest rate is an intermediate target which is controlled by monetary authority with an aim to influence commodity and financial asset prices, stabilise prices and output, as well as enhancing output growth rate. Specifically, a positive deviation of inflation from its target requires an increase in the policy rate, which leads to increase in money market interest rate as well as a fall in bond prices. This not only reduces liquidity in the economy but also bond holders’ wealth, since bond prices fall when interest rates increase. As a result, consumption and aggregate demand falls. This drives actual inflation towards the target inflation rate. Hence, the significant weight monetary authority attaches to a deviation of money market interest rate from their long term level in the quadratic loss function. A deviation of inflation from its target by 1 per cent leads to an increase in the policy rate of about 0.028 per cent. The response of monetary authority is only significant when volatility is controlled for in estimating the quadratic loss function.

Financial asset prices have the least and statistically significant weights in the estimated monetary policy quadratic loss function in all the specifications. This indicates that the Central Bank does not respond strongly to deviations of bond and equity prices. A possible explanation is that stock prices, even though have a significant effect on welfare and monetary stability, are driven by productivity, which monetary policy has little influence. However, monetary policy can respond to deviations of financial asset prices when they deviate from the discounted present value of dividends or interest earnings on bonds.

The results on the response of monetary policy to equity prices compare well with those of Bernanke & Gertler (2000); Bernanke & Kuttner (2005) in terms of sign and magnitude, even though the models are different. Whereas Bernanke & Gertler (2000) estimations yield a reduction of policy rates by 0.006 percent for Japan and 0.082 percent for USA, this paper establishes a reduction in the policy rate of 0.004 percent, in response to equity price instability. Even though the results are counter intuitive if the aim of Central Bank is to stabilise equity prices, they still explain the behaviour of Central Banks in developing economies in which the overriding monetary policy objective is achieving output and inflation stability.

A model without equity and bond prices is a proximate contrast to (Bernanke & Gertler, 2000). Results in column 6 suggest that targeting inflation, output, nominal exchange rate and interest
rate, without taking into account asset price volatility compromises effectiveness of monetary policy to reduce price instability. This is because, when asset price volatility is not considered, monetary policy has no significant effect on inflation, once output, nominal exchange rate and interest rate stability is taken into account. In this regard, targeting asset prices complements achieving output and inflation stability. Therefore, this results are contrary to findings of Bernanke & Gertler (2000), in which targeting asset prices undermine the capacity of monetary policy to stabilise output and inflation.

In as much as parameter estimates of the quadratic function provide relative weights the Central Bank attaches on output and prices in the social welfare function, the weights so estimated do not take into account optimisation decision of agents in the economy. The optimisation decision of agents in the financial and goods market as well as the government spending decisions affect actual and expected prices and output. Therefore, monetary authority can only be effective if it responds to output and prices while taking into account optimisation decisions of agents in the economy. Furthermore, agents form expectations about monetary authority’s response to deviations of output and prices from their socially desirable level to maximise social welfare (Kydland & Prescott, 1977; Di Bartolomeo & Giuli, 2011). Even though agents’ expectations affect monetary policy response to deviations of an objective variable from its target, it has little control over such expectations. Thus, in what follows, the paper next attempts to find the optimal response to deviations of output and prices from the target path, taking into account explicitly the optimisation decisions of agents.

5.1 Optimal monetary policy with output and price volatility

This section utilises the household, firm and government optimisation behavior to analyse optimal monetary policy response to instability in output, inflation as well as in equity and bond prices. An optimal policy involves a choice of weight \( \gamma \) in equation 5 given optimal portfolio holding and income growth. The one period weight estimated from monetary policy optimisation problem indicates that monetary authority should assign a penalty of 0.0000, 0.0965, 0.0358, 0.0221, 0.0018, and 0.0223 on exchange rate, output, inflation, equity, bond prices and interest rates instability respectively to maximise social welfare\(^4\). The results from the solution of optimisation problem using the numerical method suggest that monetary authority should respond to output deviating from long term trend with greatest weight compared to inflation, and asset prices. Indeed, a developing economy requires a higher rate of output growth as well as stability in income to improve welfare of the public. This is why monetary authority places greater emphasis on output target despite price stability objective being equally important. This is important for developing economies in general and particularly in Kenya where supply side constraint in the real sector have a substantial effect on inflation and financial asset price instability.

The lower weight assigned to inflation in the social welfare is consistent with the view that stabilising inflation at very low levels is not optimal in a developing economy. This is because, firstly, complete inflation stabilisation requires higher variability in the market interest rate as a result of changes in monetary policy interest rates in response to shocks that affect commodity price level. Higher variability in market interest rates disrupts allocation of credit by lenders and impedes predictions about evolution of asset prices and returns on investment by investors, thereby reducing incentive to invest (Stulz, 1986). Secondly, a developing economy’s monetary policy authority is eager to accelerate income growth to reduce poverty levels. However, accelerating income growth requires lower interest rate and a nominal exchange rate depreciation in a small open economy to increase exports. As a result, inflation deviates from zero due to lower domestic interest rate and nominal exchange rate pass-through effect to domestic prices (Divino, 2009; Monacelli, 2003).

\(^4\)This corresponds to penalties of 0.0505, 0.0018, 0.0014, 0.0001 and 0.0182 for a unit deviation from the target rate for output, inflation, equity and bond prices respectively.
This results in the large difference in the weights monetary authority place on the output growth rate gap and inflation in the optimal solution, leading to the trade-off between output gap and inflation stabilisation. Even though monetary authority has a higher propensity to increase income growth, it places substantial weight on stabilisation of bond prices compared to equity prices. This can be explained by the fact that treasury bonds traded on the NSE constitute a significant turnover of bond sales on the bonds market as well as in the entire stock market. Besides bonds trading being a significant portion of the capital market, bonds issued at the primary market change the level of liquidity and overall wealth of bond holders. This subsequently influence inflation. Therefore, substantial deviation of bond prices from their long term trend have a potential of inducing instability in the stock market and also in the entire financial sector, hence the higher weight bonds have relative to equity prices in the optimal solution.

5.1.1 Monetary Policy under Discretion Rule

The monetary authority considers expectations of the private sector regarding inflation, interest rate and output when solving the optimisation problem for the society. In particular, monetary policy achieves inflation and output gap targets if inflation and output expectation private sector are properly anchored\(^5\). In this regard, monetary authority responds to current output, inflation, and asset price instability considering the current and future expectation of the private agents. Under discretion, the monetary authority optimises the welfare function period by period. Figure 2 presents the optimal level of policy interest rate and actual policy rate obtained from solving a dynamic program of the monetary authority outline by equation 5 - 9. The optimal path for the monetary policy interest is solved using numerical methods by minimising the quadratic loss function each period with core inflation target restricted to between 3.75 percent and 7.25 percent. This is the monetary policy inflation target range set by the Central Bank of Kenya.

Even though discretion in this case results in a policy interest rate path that enables the Central Bank to achieve an inflation target, the resultant optimal output growth rate of 1 per cent is far much lower than actual average growth rate of 4.3 per cent and the target output growth rate of 5.8 per cent. This implies that the path for the optimal rate is higher than the actual policy rate, exerting a contractionary effect on the output growth that undermines achieving output growth rate objective. In as much as the path of monetary policy interest rate achieves inflation target, it is too high to be consistent with the higher income growth rate that is essential for welfare maximisation. The high interest rate reduces returns to investment that discourage meaningful investment in the economy. This leads to low output growth rate.

\(^5\)Rogoff (1985), Lucas & Stokey (1983) the expectations of the private sector regarding future monetary policy actions are rationalised that the current and future monetary policy decisions are consistent with current and future expected output gap and inflation rate.
5.1.2 Monetary Policy Commitment Rule

One of the solutions to inconsistent optimal interest rates with respect to final targets of monetary policy is commitment. Under commitment, monetary authority maximises the social welfare subject to agent’s optimisation decision and credibly commits to the resultant optimal interest rate path, without deviating from the path. Figure 3 below plots the path resulting from the optimal solution of the social welfare function under commitment.

**Figure 3: Path of interest rate under Commitment**

The optimal path of monetary policy interest rate enables optimal inflation to track actual inflation consistently overtime as shown in figure 3. The social loss value is 1198.152 with commitment to an optimal rule, which is lower compared to welfare value 3183.620 under discretion. This implies that commitment to a monetary policy rule enables the society to attain a higher welfare compared to monetary policy rule under discretion. The results are consistent with the views of King (1997), Kydland & Prescott (1977) and Svensson (1997) that commitment and discretion yield second and fourth best equilibrium respectively. The lower welfare under commitment compared to efficient and free market can be attributed to monetary policy being not able to respond to unanticipated shocks, while remaining committed to optimal rule. One of the shocks that affect the optimal solution is the exchange rate movements especially in open small open economy like Kenya. Such unanticipated shocks induce significant changes in the output gap, asset and commodity price volatility but, monetary authority has no incentive to respond to them once an optimal path for interest rate rule has been determined, as in this case in which nominal exchange rate volatility has zero penalty in the optimal solution. The implication of zero weight on exchange rate in the optimal solution is that the monetary authority cannot respond to exchange rate directly without affecting optimal welfare value under commitment. In addition, commitment to the optimal rule reduces the ability of monetary authority to take into account dynamic expectations of private agents, when consistently responding to output and asset price deviations, yet private agents’ expectations influence monetary policy target variable. These findings are consistent with views of (Divino, 2009).

---

6However, by reducing output gap and domestic inflation, monetary policy reduces demand for foreign currency, and hence, eases nominal and real exchange rate depreciation pressures. In this way, monetary policy can at least influence exchange rate indirectly under commitment in a small open economy with strong exchange rate pass-through to domestic prices.
6 Conclusion

This paper focused on optimal monetary policy response to output and financial asset price instability. The regression results indicate that monetary policy should respond to interest rate instability more strongly compared to deviation of output growth rate from the set target. Monetary policy should also respond to distortions in the equity and bond prices with lesser weight compared to exchange rate. There is also evidence that deviation of inflation from the target can be restored by smoothing interest rate adjustment towards the target interest rate. The dynamic optimisation results suggest that the output and price objectives can be achieved optimally with a consistent and credible monetary policy. In addition, the results are consistent with the regression estimates of output and inflation rate weights.

References


Appendix I

Households
c
consumption \( C_t \) real money \( M_t/P_t \), labour \( N_t \).

\[
V_t = E_t \sum_{s=0}^{\infty} \beta^s \left[ \frac{C_t^{1-\sigma}}{1-\sigma} - \frac{N_t^{1+\gamma}}{1+\gamma} + \frac{(M_t/P_t)^{1-\eta}}{1-\eta} \right] 
\]  
(10)
### Table 2: Parameters

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Definition</th>
<th>Original Value</th>
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<tbody>
<tr>
<td>$\sigma$</td>
<td>Elasticity of consumption risk aversion</td>
<td>Calibrated 0.80</td>
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<tr>
<td>$\gamma$</td>
<td>Inverse of the Frisch elasticity of labour supply</td>
<td>Calibrated 0.90</td>
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<tr>
<td>$\eta$</td>
<td>Elasticity of money demand</td>
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<tr>
<td>$\beta$</td>
<td>Discount factor</td>
<td>Calibrated 0.92</td>
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<tr>
<td>$\theta_{yt}$</td>
<td>Sensitivity of Central Bank to output gap</td>
<td>Estimated 0.80</td>
</tr>
<tr>
<td>$\theta_{ix}$</td>
<td>Sensitivity of Central Bank to inflation</td>
<td>Estimated 0.65</td>
</tr>
<tr>
<td>$\tau$</td>
<td>Aggregate tax rate</td>
<td>Estimated 0.40</td>
</tr>
<tr>
<td>$\delta$</td>
<td>Rate of depreciation</td>
<td>Estimated 0.17</td>
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<tr>
<td>$\Theta$</td>
<td>A fraction of firms with market power</td>
<td>Calibrated 0.09</td>
</tr>
<tr>
<td>$\Phi$</td>
<td>Degree of openness</td>
<td>Calibrated 0.55</td>
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<td>$\emptyset$</td>
<td>Ease of substitution</td>
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<tr>
<td>$C$</td>
<td>Contribution of deficits to inflation</td>
<td>Estimated 0.04</td>
</tr>
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Notes: This table indicates parameters for models.

---

The budget constraint is:

$$ P_t C_t + E_t \left[ \Psi_{t,t+1} B_{t+1} \right] + P_t \int_0^1 Q_t(i) Z_{t+1} \partial_i + I_t + \frac{M_{t+1}}{(1 + i_t) P_{t+1}} = W_t N_t + r_t K_t + B_t + P_t \int_0^1 (Q_t(i) + D_t(i)) Z_{t+1} \partial_i + \frac{M_t}{P_t} \tag{11} $$

where $\Psi_{t,t+1} = \frac{1}{1 + \eta}$ is the nominal interest rate. $I_t = (1 - \delta) K_t - K_{t+1}$ investment function.

Using first order conditions and adjusting prices with nominal exchange rate $\varepsilon_t$ gives:

$$ C_t = \left[ \beta \left\{ - \frac{P_t}{P_{t+1}} \varepsilon_t (1 + r_{t+1} - \delta) \right\} \right]^{\frac{-1}{\beta}} C_{t+1} \tag{12} $$

$$ N_t = \left[ C_t^{-\sigma} W_t \right]^{\frac{1}{1 - \sigma}} \tag{13} $$

$$ M_t^n = \frac{C_t^{-\sigma}}{\varepsilon_t} + \beta \frac{C_t^{-\sigma}}{(1 + i_t) \varepsilon_t P_{t+1}} \tag{13} $$

$$ Q_t = \left[ \frac{P_{t+1}}{P_t} \varepsilon_t (Q_{t+1} + D_{t+1}) \right] / (1 + r_{t+1} - \delta) $$

Log linearising and taking deviations from the steady of the consumption Euler 12 and using the idea that $y_t = c_t$ gives $y_t = E_t y_{t+1} - \frac{\beta}{\sigma} \left[ \{ r_{t+1} + (1 - \delta) \} - E_t \varepsilon_{t+1} - E_t \pi_{t+1} \right]$. $y_t = E_t y_{t+1} - \frac{\beta}{\sigma} \left[ \{ r_{t+1} + (1 - \delta) \} - E_t \varepsilon_{t+1} - E_t \pi_{t+1} \right]$ can further be summarised by using 13 $y_t = E_t y_{t+1} - \frac{\beta}{\sigma} \left[ \{ r_{t+1} + (1 - \delta) \} - E_t \varepsilon_{t+1} - E_t \pi_{t+1} \right]$.  

### Firm

Technology is Cobb Douglas production function.

$$ Y_t = K_t^a N_t^{1-a} e^{A_t} $$

$A_t = \rho A_{t-1} + \rho \epsilon$ where $\rho \epsilon = \omega \pi_{t-1} + \nu_t$ is the variance of technology shock $\epsilon$. Profit maximisation of firms is given by:

$$ \Pi_t = Y_t - W_t N_t + r_t K_t \lambda_t \left( K_t^a N_t^{1-a} e^{A_t} - Y_t \right) $$

first order condition:

$$ \frac{\partial \Pi_t}{\partial N_t} = -W_t + \lambda_t (1 - a) K_t^a N_t^{1-a} e^{A_t} = 0 $$

First order condition of profit maximization together with household utility optimisation determine equilibrium wage and real interest rate.

### Price setting by the firm.

A fraction of firms $\Theta$ have market power, that enables them to adjust price in staggered manner over time while $(1 - \Theta)$ take price as given (Calvo, 1983). Its it price setting behavior of firms that persistence of inflation and price rigidities in the economy. The Calvo price setting mechanism of a firm with market power is given as
\[
\max_{P_t} \sum_{\tau=0}^{\infty} \Theta^\tau \left\{ \Gamma_{t,t+\tau} \left( P_t^* Y_{t+\tau|t} - MC_{t+\tau} Y_{t+\tau|t} \right) \right\}
\]

\[
Y_{t+\tau|t} = \left( \frac{P_t^*}{P_{t+k}} \right)^{-\xi} C_{t+\tau}
\]

\[
\frac{\partial Y_{t+\tau|t}}{\partial P_t^*} = -E \left( \frac{P_t^*}{P_{t+k}} \right)^{-\xi-1} C_{t+\tau}
\]

\[
= -\xi \left( \frac{P_t^*}{P_{t+k}} \right)^{-\xi-1} Y_{t+\tau}
\]

\[TR_{t+\tau} + MR_{t+\tau} - MC_{t+\tau}\]

\[
P_{t+\tau} Y_{t+\tau|t} + \frac{\partial Y_{t+\tau|t}}{\partial P_t^*} - MC_{t+\tau} \frac{\partial Y_{t+\tau|t}}{\partial P_t^*}
\]

\[
= P_{t+\tau} Y_{t+\tau|t} + P_t^* \left[ -\xi \left( \frac{P_{t+\tau}}{P_t^*} \right) Y_{t+\tau} \right] - MC_{t+\tau} \left[ -\xi \left( \frac{P_{t+\tau}}{P_t^*} \right) Y_{t+\tau} \right]
\]

\[
= P_{t+\tau} Y_{t+\tau|t} \left\{ 1 + P_t^* \left[ -\xi \left( \frac{1}{P_t^*} \right) \right] - MC_{t+\tau} \left[ -\xi \left( \frac{1}{P_t^*} \right) \right] \right\}
\]

\[
= P_{t+\tau} Y_{t+\tau|t} \left( P_t^* + MC_{t+\tau} \left( \frac{\xi}{1-\xi} \right) \right)
\]

\[
E_t \sum_{\tau=0}^{\infty} \Theta^\tau \left\{ \Gamma_{t,t+\tau} \left( P_{t+\tau} Y_{t+\tau|t} \left\{ P_t^* + MC_{t+\tau} \left( \frac{\xi}{1-\xi} \right) \right\} \right) \right\}
\]

then \[E_t \sum_{\tau=0}^{\infty} \Theta^\tau \left\{ \Gamma_{t,t+\tau} \left( P_{t+\tau} Y_{t+\tau|t} \right) \right\} x \frac{P_{t+\tau}}{P_{t+\tau} + P_t^*}
\]

gives

\[
E_t \sum_{\tau=0}^{\infty} \Theta^\tau \left\{ \pi^* + MC_{t+\tau} \left( \frac{\xi}{1-\xi} \right) \pi_{t+\tau} \right\}
\]

\[
\text{note that } \Gamma_{t,t+\tau} = \beta \left[ \left( \frac{C_{t+\tau}}{C_{t+\tau}} \right)^{-\sigma} \frac{P_t^*}{P_{t+\tau}} \right]
\]

\[
E_t \sum_{\tau=0}^{\infty} \Theta^\tau \left\{ \beta \left[ \left( \frac{C_{t+\tau}}{C_{t+\tau}} \right)^{-\sigma} \frac{P_t^*}{P_{t+\tau}} \right] \left( P_{t+\tau} Y_{t+\tau|t} \right) \pi^* + MC_{t+\tau} \left( \frac{\xi}{1-\xi} \right) \pi_{t+\tau} \right\}
\]

\[
E_t \sum_{\tau=0}^{\infty} \Theta^\tau \left\{ \beta \left[ \left( \frac{C_{t+\tau}}{C_{t+\tau}} \right)^{-\sigma} \frac{P_t^*}{P_{t+\tau}} \right] \left( \pi^* + MC_{t+\tau} \left( \frac{\xi}{1-\xi} \right) \pi_{t+\tau} \right) \right\}
\]

\[
E_t \sum_{\tau=0}^{\infty} \left( \Theta \beta \right)^\tau \left[ \pi_t^* + p_t \right] = E_t \sum_{\tau=0}^{\infty} \left( \Theta \beta \right)^\tau \left[ mc_{t+\tau} + p_{t+\tau} \right]
\]

solving infinite summation and using \[
\pi_t = \frac{(1-\Theta)\pi_t^*}{(1-\Theta)(1-\Theta\beta)} mc_t + \beta E_t(\pi_{t+1})
\]

is the Philips curve.

where \[mc_t = \left( \frac{1}{1-\alpha} \right)^{1-\alpha} \left( \frac{1}{\alpha} \right)^{\alpha} \frac{W^{1-\alpha} r_{t+1}^\sigma}{A_t} \] real marginal cost. Equation states that firms maximize their discounted revenue by choosing price \[P_t^*\].

log linearising and approximating using first order Taylor expansion.

**Openness**

\[
P_t = \left[ (1-\Phi)(P_{H,t}^{1-\phi-1} + \Phi (P_{F,t}^{1-\phi})) \right]^{\frac{1}{1-\phi}}
\]

where \[\Phi\]is the degree of openness, \[\Theta\] is the substitution parameter which measures the ease of substitution between domestic and foreign goods .

log linearising price
\[ P_t = [(1 - \Phi) \phi(P_H,t) + \Phi (P_F,t)] \]

**Terms of trade**

Bilateral terms of trade between the home country \( i \) and trading partner country \( j \) is \( S_{i,t} = \frac{P_{F,t}}{P_{H,t}} \). It is the relative price index for each country. In log form \( s_t = P_{F,t} - P_{H,t} \) \( P_{F,t} \) and \( P_{H,t} \) are the foreign and the domestic price indices respectively.

\[ P_t = [(1 - \Phi) \phi(P_H,t) + \Phi (P_F,t)] = P_{H,t} + \Phi s_t \]

of one price \( P_{i,j,t} = \varepsilon_{i,t} P_{j,t} \) is the purchasing power parity, stating that foreign price should be equal to domestic price in domestic currency. \( \varepsilon_t = \psi \varepsilon_{t-1} + \omega_t h_t \) is the nominal exchange rate which follows an Auto regressive process of order 1 (AR1). In managed floating regimes exchange rate movements approximate AR 1 process (Funke et al., 2011). \( \omega_t = \rho_{\omega,t} \omega_{t-1} + \nu_t \) stochastic volatility process in the nominal exchange rate. \( h_t \sim N(0,1) \) \( \nu_t \sim N(0,1) \).

foreign price \( P_{F,t} = \int_0^t (e_{i,t} + P_{j,t}) \partial t \)

Real exchange rate \( \mathbb{R} = \frac{P_t^i}{P_t} \)

\[ \mathbb{R} = \int_0^t (e_{i,t} + P_{j,t} - P_t) \partial t \]

\[ = e_t + P_t^* - P_t \]

\[ = s_t + P_{H,t} - P_t \]

\[ = (1 - \Phi)s_t \]

world income \( y_t^* \) is an autoregressive process of order 1.

\( y_t^* = \psi y_{t-1}^* + \zeta_t \)

**Appendix II**

\[ V_t = E_t \sum_{i=0}^{\infty} \beta^i \left[ C_t^{1-\sigma} \frac{N_t^{1+\gamma}}{1+\gamma} + M_t^{1-\eta} \right] \]

\[ C_t^{1-\sigma} = C_t^{1-\sigma} + C_t^{1-\sigma} \left[ C_t + \frac{(1 - \sigma)C_t^2}{2} \right] + \gamma^3 \]

\[ N_t^{1+\gamma} = N_t^{1+\gamma} + N_t^{1+\gamma} \left[ N_t + \frac{(1 + \gamma)N_t^2}{2} \right] + \gamma^3 \]

\[ M_t^{1-\eta} = M_t^{1-\eta} + M_t^{1-\eta} \left[ M_t + \frac{(1 - \eta)M_t^2}{2} \right] + \gamma^3 \]

Second order Taylor approximation for output at zero state.

\[ Y_t = \bar{Y} + \bar{Y} Y_t + \frac{1}{2} \bar{Y} Y_t^2 + \gamma^3 \]

Consumption \( \bar{C} \) is given by \( \bar{C} = \bar{Y} - \bar{S} \)

\[ C_t^{1-\sigma} = \bar{C}_t^{1-\sigma} + \bar{C}_t^{1-\sigma} \left[ \bar{Y}_t - \bar{S}_t + \frac{(1 - \sigma) (\bar{Y}_t - \bar{S}_t)^2}{2} \right] + \gamma^3 \]

\[ N_t = \frac{Y_t}{A_t} \int_0^t \left( \frac{P_{H,t}(i)}{P_{H,t}} \right)^{-\xi} \partial i \]

let \( d_t = \int_0^t \left( \frac{P_{H,t}(i)}{P_{H,t}} \right)^{-\xi} \partial i \) The \( n_t = y_t + d_t - a_t \) in logarithm form. let also \( P_{H,t}(i) = P_{H,t}(i) - P_{H,t} \) by taking the logarithm. A second order Talyor series approximation after taking logarithm. Hence:
\[
\left( \frac{P_{H,t}(i)}{P_{H,t}} \right)^{1-\xi} = \exp \left[ (1-\xi)P'_{H,t}(i) \right]
\]

\[
= 1 + (1-\xi)P'_{H,t}(i) + \frac{1}{2}(1-\xi)^2 \left( P'_{H,t}(i) \right)^2 + \gamma^3
\]

\[
E_i \{ P'_{H,t}(i) \} = \frac{1}{2}(\xi-1)E_i \{ P'_{H,t}(i) \}^2
\]

\[
\int_0^1 \left( \frac{P_{H,t}(i)}{P_{H,t}} \right)^{-\xi} \, \partial i = 1 - \xi E_i \{ P'_{H,t}(i) \} + \frac{1}{2} \xi^2 E_i \{ P'_{H,t}(i) \}^2 + \gamma^3
\]

\[
= 1 + \xi E_i \{ P'_{H,t}(i) \}^2 + \gamma^3
\]

\[
= 1 + \frac{\xi}{2} Var_i \{ P'_{H,t}(i) \} + \gamma^3
\]

and therefore \( d_t = \int_0^1 \left( \frac{P_{H,t}(i)}{P_{H,t}} \right)^{-\xi} \, \partial i = \frac{\xi}{2} Var_i \{ P'_{H,t}(i) \} + \gamma^3 \)

\[
N_t^{1+\gamma} = (1-\alpha) \left[ d_t + \frac{(1+\gamma)(y_t)^2}{2} \right] + tip + \gamma^3
\]

\( tip \) consists of \( a_t, d_t a_t, y_t d_t a_t \) and \( y_t \) which cannot be influenced by monetary policy.

Second-order Taylor approximation for equity and bond price.

Financial assets consist of money bonds and equity.

\[
\Psi = M + B_t \int_0^1 \left( \frac{F_{H,t}(i)}{F_{H,t}} \right)^{-\epsilon} \, \partial i + Q_t \int_0^1 \left( \frac{Z_{K,t}(i)}{Z_{K,t}} \right)^{-\omega} \, \partial i
\]

Following a similar procedure as inflation, equity and bond price approximations are,

\[
\tilde{B}_t = \int_0^1 \left( \frac{F_{H,t}(i)}{F_{H,t}} \right)^{-\epsilon} \, \partial i = 1 + \frac{\epsilon}{2} Var_i \{ F'_{H,t}(i) \} + \gamma^3
\]

\[
\tilde{Q}_t = \int_0^1 \left( \frac{Z_{K,t}(i)}{Z_{K,t}} \right)^{-\omega} \, \partial i = 1 + \frac{\omega}{2} Var_i \{ Z'_{K,t}(i) \} + \gamma^3
\]

\[
M_t^{1-\eta} = M_t^{1-\eta} \left[ \tilde{B}_t + \tilde{B}_t + \tilde{Q}_t + \tilde{Q}_t + \frac{(1-\eta)(\tilde{B}_t + \tilde{B}_t + \tilde{Q}_t + \tilde{Q}_t)^2}{2} \right] + \gamma^3
\]

\[
= \alpha \left[ \tilde{B}_t + \tilde{B}_t + \tilde{Q}_t + \tilde{Q}_t + \frac{(1-\eta)(\tilde{B}_t + \tilde{B}_t + \tilde{Q}_t + \tilde{Q}_t)^2}{2} \right] + \gamma^3
\]

substituting all the terms in the utility function

\[
V_t = E_t \sum_{t=0}^\infty \beta^t \left[ \tilde{B}_t + \tilde{B}_t + \tilde{Q}_t + \tilde{Q}_t + \frac{(1-\eta)(\tilde{B}_t + \tilde{B}_t + \tilde{Q}_t + \tilde{Q}_t)^2}{2} \right] + \gamma^3
\]

\[
= E_t \sum_{t=0}^\infty \beta^t \left[ \tilde{B}_t + \tilde{B}_t + \tilde{Q}_t + \tilde{Q}_t + \frac{(1-\eta)(\tilde{B}_t + \tilde{B}_t + \tilde{Q}_t + \tilde{Q}_t)^2}{2} \right] + \gamma^3
\]

\[
= E_t \sum_{t=0}^\infty \beta^t \left[ \tilde{B}_t + \tilde{B}_t + \tilde{Q}_t + \tilde{Q}_t + \frac{(1-\eta)(\tilde{B}_t + \tilde{B}_t + \tilde{Q}_t + \tilde{Q}_t)^2}{2} \right] + \gamma^3
\]
where $\Gamma = \frac{(1-\Theta)}{(\Theta)}$ from the Keynesian Philips curve.

Then the continuous counterpart is

$$L = E_t \int_{t=0}^{\infty} e^{-\delta t} \left( \frac{(1-\alpha)}{2} \pi_{H,t}^2 + \frac{\alpha(1-\sigma) - (1-\alpha)(1+\gamma)(yt)^2}{2} + \frac{\alpha \omega \hat{Q}_t^2}{2} + \alpha \frac{\epsilon \hat{B}_t^2}{2} \right) + \text{tip} + \Gamma$$

$$\text{Maximise} = \int_{t=0}^{\infty} e^{-\delta t} \left( \gamma_\pi \pi_{H,t}^2 + \gamma_y (yt)^2 + \gamma_Q \hat{Q}_t^2 + \gamma_B \hat{B}_t^2 \right)$$

Equation 16 is the state equation, and $L$ is the variable to be maximised. $\gamma_\pi$, $\gamma_y$, $\gamma_Q$, $\gamma_B$ are contributions of inflation, income, equity price and debt instability to social loss. They are also weights of respective variable in the social loss function. Equations 17-22 are decision equation which influence the state equation. The decision variable is $i$ interest rate. That is $i$ is changed to ensure that $L$ is maximised subject to equation 17-22. $B$ is the debt level, $y$ income, $\pi$ inflation, $x$ expenditure, $e$ output shock, $\beta$ sensitivity of change in income to spending, $b$ sensitivity of output to inflation stability, $Q$ equity price, $t$ tax rate. $r$ exchange rate. The dots above a variable indicate the variable is a first derivative with respect to time.

\[ \delta \text{ discount factor, } t \text{ time.} \]

\[ \gamma_\pi = \frac{(1-\alpha)}{1}, \gamma_y = \alpha(1-\sigma) - (1-\alpha)(1+\gamma), \gamma_Q = \alpha \omega, \gamma_B = \alpha \epsilon \]

\[ \dot{\gamma}_{t} = \beta x_t + b((1 + i_t) - \pi_{t+1}) + e_t \quad (17) \]

\[ \dot{\pi}_{t} = ((1 + i_t) - \pi_{t+1}) + C x_t \quad (18) \]

\[ \dot{Q}_{t} = \frac{(Q_{t+1} \pi_{t+1} \epsilon_t)}{1 + i_t} \quad (19) \]

\[ \dot{B}_{t} = \frac{B_{t-1}}{(1 + i_t)} \quad (20) \]

\[ \dot{x}_{t} = \frac{B_{t-1}(1 + i) - B_t}{(1 + i_t)} + \tau y_t \quad (21) \]

\[ \dot{\epsilon}_{t} = -i \quad (22) \]

\[ i > 0 \]
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<th>Prob.</th>
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Notes: In this regression the dependent variable is the deviation of repo rate from its trend. Output gap is the deviation of actual output from the potential output, which is the trend. Output growth rate is squared deviation from target growth rate. (Output is equal to income from national income account.) Inflation is the squared deviation from the average target inflation rate of 5 per cent. Equity, bond prices and interest are squared deviation from their long term trends. With respect to bond prices the long term trend is consistent with the yield curve.