

Applying Monetary-Fiscal Policy Interactions: Part II

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Overview

- ▶ These notes discuss empirical issues that arise with monetary-fiscal policy interactions
 1. Observational equivalence
 2. Two problems with surplus-debt regressions that arise from the existence of the forward-looking bond-valuation condition
 3. Confronting fiscal data

The Issue

1. **Observational Equivalence (OE)**: two or more underlying entities are indistinguishable on the basis of their observable implications
2. In econometrics, two *structures* are observationally equivalent if they imply the same probability distribution of data
3. Consider two distinct policy regimes: **M**: active M/passive F and **F**: passive M/active F
4. **M** and **F** are OE if they produce equilibrium data with the same covariance generating process
5. Two structures, θ_q and θ_r , are OE if and only if $F(\gamma|\theta_q) = F(\gamma|\theta_r)$ for all γ

The Issue

1. There is related idea: structure q is **nearly observational equivalence** to r if $F(\cdot|\theta_q)$ is “close to” $F(\cdot|\theta_r)$
2. Near equivalence of members of the sequence $\{\theta_k\}$ to θ_r implies that for any $\varepsilon > 0$ we can find a k such that $F(\gamma|\theta_k) - F(\gamma|\theta_r) < \varepsilon$ for all γ [Faust(1996)]
3. Near OE preserves many of the implications of strict OE
4. For practical empirical purposes, near OE is most relevant
5. Equivalence makes it difficult to identify

Result #1

- ▶ Cochrane (2010,2011) shows that indeterminate equilibria can generate time series that are indistinguishable from determinant ones
- ▶ Employs a Fisherian model

$$R_t = r + E_t \pi_{t+1}$$

$$R_t = r + \alpha \pi_t + x_t$$

$$x_t = b(L) \varepsilon_{x,t}$$

R : nominal interest rate, π : inflation rate, r constant real rate, x_t is square summable, $\sum_j b_j^2 < \infty$

Result #1

Proposition

(Cochrane) For any stationary time series process for $\{R_t, \pi_t\}$ that solves

$$E_t \pi_{t+1} = \alpha \pi_t + x_t \quad (1)$$

and for any α , one can construct an x_t process that generates the same process for the observables $\{R_t, \pi_t\}$ as a solution to (1) using the alternative α . If $\alpha > 1$, the observables are generated as the unique bounded forward-looking solution. Given an assumed α and the process $\pi_t = a(L)\varepsilon_{x,t}$, where $a(L)$ is a polynomial in the lag operator L , we can construct $x_t = b(L)\varepsilon_{x,t}$ with

$$b_j = a_{j+1} - \alpha a_j$$

or

$$b(L) = (L^{-1} - \alpha)a(L) - a(0)L^{-1} \quad (2)$$

Result #1

Proof.

To prove the proposition note that for $\alpha > 1$ and $x_t = b(L)\varepsilon_{x,t}$, the unique π_t is given by

$$\pi_t = \left(\frac{Lb(L) - \alpha^{-1}b(\alpha^{-1})}{1 - \alpha L} \right) \varepsilon_{x,t} = a(L)\varepsilon_{x,t} \quad (3)$$

For $\alpha < 1$, the equilibrium will not be uniquely determined and one may construct a π_t solved “backward” to obtain, $\pi_t = x_t/(1 - \alpha L)$. Specifying $b(L)$ as (2) and substituting into (3) gives $\pi_t = x_t/(1 - \alpha L)$. Under this restriction, the inflation process generated by $\alpha < 1$ will be identical to the inflation process generated by $\alpha > 1$. Proving the converse (starting with $\alpha < 1$ and showing that there exists an $\alpha > 1$ that generates the observational equivalence) is straightforward since one can always write the solution as $\pi_{t+1} = \alpha\pi_t + x_t + \delta_{t+1}$, where δ_{t+1} is an arbitrary shock. In this case, setting $\delta_{t+1} = a_0\varepsilon_{t+1}$ delivers the result. Note that because $R_t = r + E_t\pi_{t+1}$, matching the inflation process also delivers an equivalence in the nominal interest rate. \square

Meaning of the Proposition

- ▶ Illustrates that important identifying restrictions are imposed through the assumed exogenous processes
- ▶ Cross-equation restrictions in (3) show tight relationship between exogenous & endogenous variables
- ▶ Cochrane (2011) emphasizes that for an exogenous process like (2) cannot tell if observed time series generated by determinate or indeterminate eqm
- ▶ Cochrane's proposition relies on indeterminate equilibria taking particular form
- ▶ But there are an infinite number of indeterminate equilibria
- ▶ Now show observational equivalence between *unique* equilibria from decoupled determinacy regions

Result #2

- ▶ Example of strict OE
- ▶ Extend Fisherian economy to include fiscal policy
- ▶ The log-linearized equilibrium equations are

$$R_t = \pi_{t+1} \quad (4)$$

$$b_t + (\beta^{-1} - 1)s_t = \beta^{-1}b_{t-1} + \beta^{-1}(R_{t-1} - \pi_t) \quad (5)$$

where we have used that in steady state,
 $s/b = \beta^{-1} - 1$; equations hold for $t \geq 0$, given
 $R_{-1}b_{-1} > 0$

- ▶ Add linearized policy rules

$$R_t = \alpha\pi_t \quad (6)$$

$$s_t = \gamma b_{t-1} \quad (7)$$

Result #2

- ▶ Substitute rules (6) & (7) into (4) & (5) to get system

$$\pi_{t+1} = \alpha\pi_t, \quad t \geq 0$$

$$b_t + \beta^{-1}\pi_t = \gamma^*b_{t-1} + \alpha\beta^{-1}\pi_{t-1}, \quad t \geq 1$$

$$b_0 + (\beta^{-1} - 1)s_0 = \beta^{-1}(b_{-1} + R_{-1})$$

where $\gamma^* \equiv \beta^{-1} - \gamma(\beta^{-1} - 1)$

- ▶ Consider special case where $b_{-1} = R_{-1} = 0$ (not necessary)

Result #2

- ▶ With $\alpha > 1$ & $\gamma > 1$, unique bounded eqm is

$$\pi_t = 0, \quad R_t = 0, \quad b_t = 0, \quad s_t = 0, \quad \text{for all } t \geq 0$$

- ▶ Can implement eqm in (11) with PM/AF rules

$$R_t = 0, \quad s_t = 0$$

for $t \geq 0$ (these rules emerge when $\alpha = \gamma = 0$)

- ▶ With constant r , the MP rule implies $\pi_{t+j} = 0, j \geq 1$
- ▶ $R_t = 0$ & $s_t = 0$ for $t \geq 0$ implies debt process

$$b_t = \beta^{-1}b_{t-1} - \beta^{-1}\pi_t \tag{8}$$

- ▶ Iterating forward and taking expectations yields

$$b_t = \sum_{j=1}^{\infty} \beta^j \pi_{t+j} = 0$$

- ▶ If $b_t = 0$, then (8) implies that $\pi_t = 0$

The Literature

- ▶ Three approaches to observational equivalence
 1. Ignore it due to ignorance [Canzoneri, Cumby, Diba]
 2. Acknowledge it and push one interpretation [Cochrane]
 3. Acknowledge it and try to break it
- ▶ Those who ignore it seem to think you can “test” if eqm condition holds

$$\frac{B_{t-1}}{P_t} = \sum_{T=t}^{\infty} E_t q_{t,T} S_T$$

- ▶ if it fails to hold in data, “reject” fiscal theory
- ▶ Only one problem with this: eqm condition holds in both regimes
- ▶ Some DSGE evidence

Traum & Yang (2011)

- ▶ A medium-size NK model estimated to U.S. postwar data
- ▶ Includes only one-period government bonds & income taxes

	Log Bayes Factor for Regime M
1955–1966	9.8
1967–1979	7.9
1984–2007	22

- ▶ Consistently strong evidence in favor of M
- ▶ Very strong evidence in favor of M post–1982

Tan (2014)

- ▶ Smaller scale NK model estimated to U.S. postwar data
- ▶ Includes only one-period & long bonds & lump-sum taxes

	Log Bayes Factor for Regime M	
	Short	Long
1955–1966	85.6	35.3
1967–1979	240.2	49.1
1984–2007	86.9	−5.8

- ▶ Consistently very strong evidence in favor of M
- ▶ Exception is post–1984 with long debt

Leeper, Traum & Walker (2017)

- ▶ A medium-size NK model estimated to U.S. postwar data
- ▶ Includes long government bonds & factor taxes & steady state tax rates

	Log Bayes Factor for Regime M
1955–2014	–8
1955–2007	11
1955–1979	4
1982–2007	12

- ▶ Far weaker evidence in favor of M
- ▶ Generally, data do not favor one regime over the other

Wrap Up

- ▶ Surprising that Regimes M & F can display OE
- ▶ Exogenous shocks to MP & FP have starkly different impacts in the two regimes
- ▶ What's going on?
- ▶ Exogenous shocks are not observables
- ▶ In a stochastic model, OE entails finding shock processes that deliver the same covariance generating process for **endogenous** variables
 - ▶ e.g., shocks might be AR(1) in M, but ARMA(2,3) in F to deliver OE
 - ▶ in Cochrane's prop, we are solving for the b_j 's that deliver identical $\{\pi_t\}$
- ▶ If impose identical processes across regimes, no OE: but get identification from strong assumptions about unobservables
- ▶ Much work remains to be done on this topic

Surplus-Debt Regressions I

- ▶ Many studies follow Bohn (1998) to estimate fiscal reaction functions of the form

$$s_t = \gamma b_{t-1} + \mu_t$$

s and b : primary surplus and government debt as shares of GDP; $\mu_t = \delta X_t + \varepsilon_t$, X “controls” and ε fiscal disturbance

- ▶ Bohn interprets positive estimates of γ to mean “the government is taking actions—reducing noninterest outlays or raising revenue—that counteract the changes in debt”
- ▶ those fiscal actions, Bohn argues, imply that fiscal policy is sustainable
- ▶ Regressions like this play key role in policy analysis
 - ▶ underpin IMF’s fiscal space calculations
 - ▶ basis for literature that tests for sustainability

Scrutinizing Surplus-Debt Regressions

- ▶ Estimates seem justified econometrically
 - ▶ b_{t-1} determined at $t - 1$, should be predetermined for s_t
 - ▶ this view reflects the “backward” interpretation of debt: accumulation of past gross deficits
 - ▶ predeterminedness requires $E[\varepsilon_t | b_{t-1}] = 0$
- ▶ What could be wrong with this econometric argument?
 - ▶ policy rule is just one of many equations describing equilibrium
 1. asset-pricing relations determine bond yields
 2. monetary policy determines relationship between inflation & bond yields
 3. bond valuation equation: “forward” representation determines *value* of government debt

Scrutinizing Surplus-Debt Regressions

- ▶ Bond valuation: embeds asset prices & optimizing behavior

$$b_{t-1} = E_{t-1} \sum_{T=t}^{\infty} q_{t-1,T} s_T$$

$b_{t-1} = B_{t-1}/P_{t-1}$, q real discount factor, s primary surplus

- ▶ *in any equilibrium* real debt positively correlated with expected surpluses (not about causality)
- ▶ if ε_t serially correlated, $E[\varepsilon_t | b_{t-1}] \neq 0$
- ▶ Monetary policy: if the price of bonds, $1/P_{t-1}$, depends on expected surpluses
 - ▶ debt-GDP ratio depends on future surpluses
 - ▶ if ε_t serially correlated, $E[\varepsilon_t | b_{t-1}] \neq 0$
- ▶ Single-equation estimates of γ cannot control for these features of the general equilibrium

Illustrative Model

- ▶ Cashless, constant-endowment, infinite-horizon
 - ▶ $1/\beta$ constant gross real interest rate
 - ▶ government purchases zero, issues nominal bonds that sell at price $1/R_t$, levies lump-sum taxes
 - ▶ log-linearized around deterministic steady state

$$\text{Fisher relation : } R_t = E_t \pi_{t+1}$$

$$\text{Monetary policy : } R_t = \alpha \pi_t + \varepsilon_t^R$$

$$\text{Fiscal policy : } s_t = \gamma b_{t-1} + \varepsilon_t^S$$

$$\text{Government budget : } b_{t-1} = \beta b_t - \beta R_t + \pi_t + (1 - \beta) s_t$$

$\varepsilon^R, \varepsilon^S$ exogenous $AR(1)$ with $0 \leq \rho_R, \rho_S < 1$ & innovations $\xi^R, \xi^S \sim N(0, 1)$

- ▶ Two regimes deliver unique bounded equilibria
 - $|\alpha| > 1, |\gamma| > 1$: active monetary/passive fiscal “Regime M”
 - $|\alpha| < 1, |\gamma| < 1$: passive monetary/active fiscal “Regime F”

Model Solution

- ▶ Regime M: $\alpha > 1, \gamma > 1$

$$\pi_t = -\frac{1}{\alpha - \rho_R} \varepsilon_t^R$$

$$b_{t-1} = (1 - \Gamma L)^{-1} \left[\frac{1 - \beta \rho_R}{\beta(\alpha - \rho_R)} \varepsilon_{t-1}^R - (\beta^{-1} - 1) \varepsilon_{t-1}^S \right]$$

$$s_t = \gamma b_{t-1} + \varepsilon_t^S$$

$$\Gamma \equiv \beta^{-1} - \gamma(\beta^{-1} - 1) < 1$$

- ▶ Regime F: $0 \leq \alpha < 1, \gamma = 0$

$$\pi_t = b_{t-1} - \frac{1 - \beta}{1 - \beta \rho_S} \varepsilon_t^S$$

$$b_{t-1} = (1 - \alpha L)^{-1} \left[\varepsilon_{t-1}^R + \left(\frac{(1 - \beta)(\rho_S - \alpha)}{1 - \beta \rho_S} \right) \varepsilon_{t-1}^S \right]$$

$$s_t = \varepsilon_t^S$$

Using the Model

- ▶ Treat the model as the data-generating process
- ▶ Use equilibrium $\{s_t, b_{t-1}\}$ in each regime to compute the linear projection

$$\mathcal{P}[s_t | b_{t-1}] = \phi b_{t-1}$$

- ▶ Note that can write

$$\phi = \frac{E(s_t b_{t-1})}{E b_{t-1}^2} = \gamma + \frac{E(b_{t-1} \varepsilon_t^S)}{E b_{t-1}^2} = \gamma + \frac{\text{cov}(b_{t-1}, \varepsilon_t^S)}{\text{var}(b_{t-1})}$$

- ▶ Ask if $\phi = \gamma$
 - ▶ $\text{cov}(b_{t-1}, \varepsilon_t^S) / \text{var}(b_{t-1})$ is the bias
 - ▶ turns out the bias depends on policy regime and policy parameters
- ▶ Note: equilibrium real debt an $AR(2)$ in innovations to policy shocks

Bias in Regime M

$$\phi = \gamma - (1 - \Gamma^2) \frac{\frac{\rho_S(\beta^{-1} - 1)}{1 - \Gamma\rho_S}}{(\beta^{-1} - 1)^2 \left(\frac{1 + \Gamma\rho_S}{1 - \Gamma\rho_S}\right) + \left(\frac{\beta^{-1} - \rho_R}{\alpha - \rho_R}\right)^2 \left(\frac{1 + \Gamma\rho_R}{1 - \Gamma\rho_R}\right) \frac{\text{var}(\varepsilon_t^R)}{\text{var}(\varepsilon_t^S)}}$$

- ▶ Bias disappears if $\rho_S = 0$: no change in expectations
- ▶ Bias negative if $0 < \rho_S < 1$: serial correlation of shocks dominates endogenous response to debt in short run
- ▶ Size of bias increases with α : more aggressive MP reduces debt volatility
- ▶ Bias increasing in $\text{var}(\varepsilon^S)/\text{var}(\varepsilon^R)$: more volatile FP makes bias worse
- ▶ In regime M: $\gamma > 1$ and estimates will tend to find *larger* values, but this doesn't affect qualitative inferences of fiscal behavior

Bias in Regime F

$$\phi = \gamma + (1 - \alpha^2) \frac{\frac{\rho_S(1-\beta)(\rho_S-\alpha)}{(1-\beta\rho_S)(1-\alpha\rho_S)}}{\left(\frac{(1-\beta)(\rho_S-\alpha)}{1-\beta\rho_S}\right)^2 \left(\frac{1+\alpha\rho_S}{1-\alpha\rho_S}\right) + \left(\frac{1+\alpha\rho_R}{1-\alpha\rho_R}\right) \frac{\text{var}(\varepsilon_t^R)}{\text{var}(\varepsilon_t^S)}}$$

- ▶ In this case, $\gamma = 0$ so $\phi = \text{bias}$
- ▶ Bias disappears if $\rho_S = 0$: no change in expectations
- ▶ $\text{sign}(\text{bias}) = \text{sign}(\rho_S - \alpha)$
 - ▶ $\rho_S > \alpha$: serial correlation dominates effect on bond prices, so b_{t-1} moves with ε_{t-1}^S
 - ▶ $\alpha > \rho_S$: effect on bond prices dominates serial correlation, so b_{t-1} moves against ε_{t-1}^S
- ▶ Bias increasing in $\text{var}(\varepsilon^S)/\text{var}(\varepsilon^R)$: more volatile FP makes bias worse
- ▶ In regime F: $\gamma = 0$ but estimates may find either positive or negative values, which could affect qualitative inferences of fiscal behavior

Summary

- ▶ Regressions most likely to be unreliable in cases where surpluses *do not* respond to debt
 - ▶ if $H_0 : \gamma = 0$, reason to believe may reject even when hypothesis is true
 - ▶ type I error
- ▶ This exposition simply *illustrates* that single-equation surplus-debt regressions may be unreliable
- ▶ This becomes a quantitative question: how big is the bias?
- ▶ But also a qualitative question: what monetary-fiscal regime prevails?
- ▶ Can we use data to distinguish between regime M & regime F?

Surplus-Debt Regressions II

- ▶ Two types of surpluses & government bonds
 1. fully backed (“ordinary”)
 2. unbacked (“emergency”)
- ▶ The government budget identity is

$$\frac{B_t^e + B_t^o}{P_t} + s_t^e + s_t^o = \frac{(1 + i_{t-1})(B_{t-1}^e + B_{t-1}^o)}{P_t}$$

total debt $B_t = B_t^e + B_t^o$; total surplus $s_t = s_t^o + s_t^e$

- ▶ Model economy with representative HH
 - ▶ constant endowment, cashless, no govt purchases
 - ▶ utility depends only on consumption, c_t
 - ▶ nominal debt, B_t , pays gross interest, $1 + i_t$
 - ▶ primary surplus, s_t , is lump-sum taxes net of transfers

Model

- ▶ HH's intertemporal budget constraint in period t

$$E_t \sum_{T=t}^{\infty} q_{t,T} c_T = \frac{(1 + i_{t-1})B_{t-1}}{P_t} + E_t \sum_{T=t}^{\infty} q_{t,T} [y_T - s_T]$$

- ▶ Yields an equilibrium condition at t

$$\frac{(1 + i_{t-1})(B_{t-1}^o + B_{t-1}^e)}{P_t} = E_t \sum_{j=0}^{\infty} \beta^j s_{t+j} = s_t^o + s_t^e + \beta E_t PV(s^o + s^e)$$

- ▶ Ordinary & emergency distinguished by fiscal rules
 - ▶ ordinary debt fully backed by future surpluses
 - ▶ marginal changes in emergency debt unbacked

$$s_t^o = \bar{s}^o + \gamma \left[\frac{(1 + i_{t-1})B_{t-1}^o}{P_t} - \bar{b}^o \right]$$

$\{s_t^e\}$ a stationary stochastic process with innovation ε_t

- ▶ Assume MP pegs nominal rate: $i_t = \bar{i}$, all t

Equilibrium

- ▶ s^e : “emergency” net taxes—unbacked
 - ▶ $ds_t^e < 0$ & set $\beta d(PV(s^e)) = 0 \Rightarrow$ increase nominal wealth/demand
- ▶ s^o : “ordinary” net taxes—backed by future taxes
 - ▶ $ds_t^o = -\beta d(PV(s^o)) \Rightarrow$ no change in wealth/demand
- ▶ Ricardian equiv \Rightarrow all “ordinary” terms cancel *for any* $\{P_t\}$ sequence (not just eqm prices)
- ▶ Reduces eqm condition to involve only “emergency” terms

$$\frac{(1 + \bar{i})B_{t-1}^e}{P_t} = E_t \sum_{j=0}^{\infty} \beta^j s_{t+j}^e \quad (9)$$

- ▶ Determines eqm price level & nominal aggregate demand
 - ▶ shocks that raise s^e are deflationary

Equilibrium

- ▶ Given eqm $\{P_t\}$ from (9), ordinary debt evolves as

$$\frac{B_t^o}{P_t} = (\gamma \bar{b}^o - \bar{s}^o) + (1 - \gamma) \left[\frac{(1 + i) B_{t-1}^o}{P_t} \right]$$

γ chosen to stabilize ordinary debt: $\gamma > 1 - \beta$

- ▶ What does the *aggregate* fiscal rule look like?
- ▶ Remember that the “e”/“o” distinction does not typically occur in actual data
- ▶ We have data on aggregate surpluses & debt
- ▶ Let steady-state real debt levels be

$$\bar{b}^o \equiv \left(\frac{\bar{B}^o}{\bar{P}} \right), \quad \bar{b}^e \equiv \left(\frac{\bar{B}^e}{\bar{P}} \right), \quad \bar{s} = \bar{s}^o + \bar{s}^e$$

Aggregate Fiscal Rule

- Write the fiscal rule as

$$s_t^o + s_t^e = \bar{s}^o + s_t^e + \gamma(1 + \bar{i}) \left[\frac{B_{t-1}^o}{P_t} + \frac{B_{t-1}^e}{P_t} - \frac{\bar{b}^o}{1 + \bar{\pi}} - \frac{B_{t-1}^e}{P_t} \right] \quad (10)$$

- Suppose emergency surpluses obey

$$s_t^e = \bar{s}^e + \varepsilon_t, \quad E_t \varepsilon_{t+1} = 0$$

- From eqm condition (9) & steady state relation $\bar{s}^e = (\beta^{-1} - 1)\bar{b}^e$, it follows that

$$\left(\frac{1 + \bar{i}}{1 + \pi_t} \right) b_t^e - \left(\frac{1 + \bar{i}}{1 + \bar{\pi}} \right) \bar{b}^e = \varepsilon_t \quad (11)$$

- Use (11) to replace the second B_{t-1}^e/P_t term in (10)

Aggregate Fiscal Rule

- ▶ With that replacement, the aggregate fiscal rule becomes

$$s_t^o + s_t^e = \bar{s}^o + \bar{s}^e + \gamma(1 + \bar{i}) \left[\frac{b_{t-1}^o + b_{t-1}^e}{1 + \pi_t} - \frac{\bar{b}^o + \bar{b}^e}{1 + \bar{\pi}} \right] + \gamma(1 + \bar{i})\varepsilon_t$$

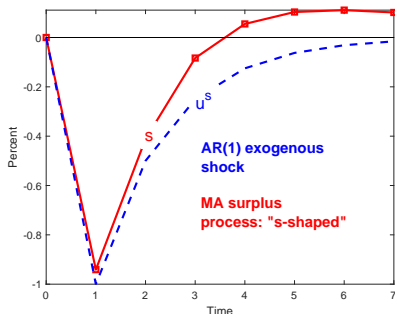
or

$$s_t = \bar{s} + \gamma(1 + \bar{i}) \left[\frac{B_{t-1}}{P_t} - \frac{\bar{b}}{1 + \bar{\pi}} \right] + \xi_t \quad (12)$$

- ▶ If $\gamma > 1 - \beta$, infer fiscal behavior is passive
 - ▶ the same condition that stabilizes ordinary debt
 - ▶ infer that shocks that raise s do not affect price level
- ▶ Can generalize $\{s_t^e\}$ process and (12) will take different forms, but message that would infer aggregate fiscal behavior is passive remains

Confronting Fiscal Data

- ▶ Fiscal policy poses a host of new issues relative to MP
 - ▶ “Fiscal Analysis is Darned Hard” discusses many
- ▶ Here focus narrowly on a topic Cochrane emphasizes: “*s*-shaped” primary surplus

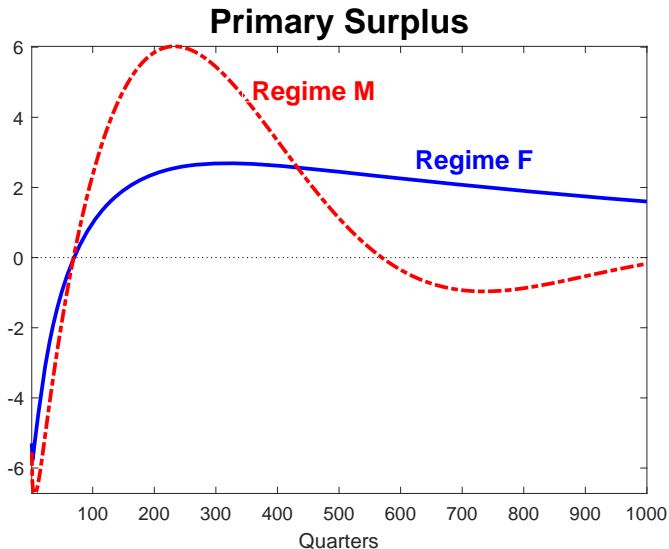


- ▶ Deficits tend to be followed by surpluses

s -shaped Surplus

- ▶ For good institutional reasons, surpluses are *not* $AR(1)$
 - ▶ $AR(1)$ convenient for theory
 - ▶ disaster for interpreting data
- ▶ Some reasons
 1. Governments can sell debt only if investors assured debts will be paid off
 2. Surpluses strongly cyclical: low in recessions, high in recoveries
 3. Even when FP does not adjust instruments in response to debt, tax codes & spending programs still remain in place
 4. An $AR(1)$ denies all these
- ▶ Medium-scale DSGE models with sufficient fiscal detail & fit to data estimate s -shape, but at *very* low frequency
 - ▶ holds regardless of monetary-fiscal regime

s-shaped Surplus From Data



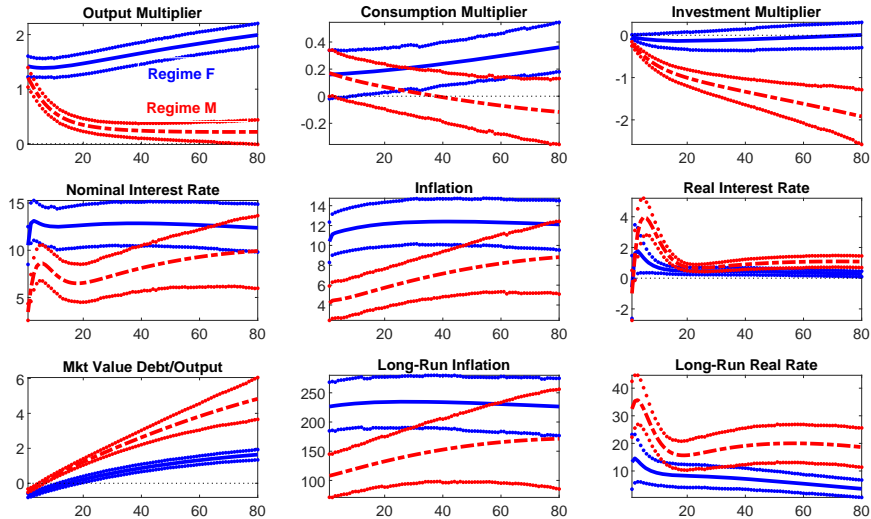
Following government purchase increase.

Source: Leeper-Traum-Walker (2017)

Policy Identification

- ▶ Despite observational equivalence, much at stake in identifying policy regime
- ▶ My approach to observational equivalence:
 1. Continue to work on identifying policy
 2. In meantime, acknowledge OE and be agnostic
- ▶ Agnosticism: examine policy impacts in both Regime M & F
- ▶ If data cannot choose between regimes, policy makers need to know it
- ▶ Prevailing regime becomes part of our uncertainty
- ▶ Example: government purchase multipliers

Fiscal Impacts Conditional on Regime



Following government purchase increase.

Source: Leeper-Traum-Walker (2017)

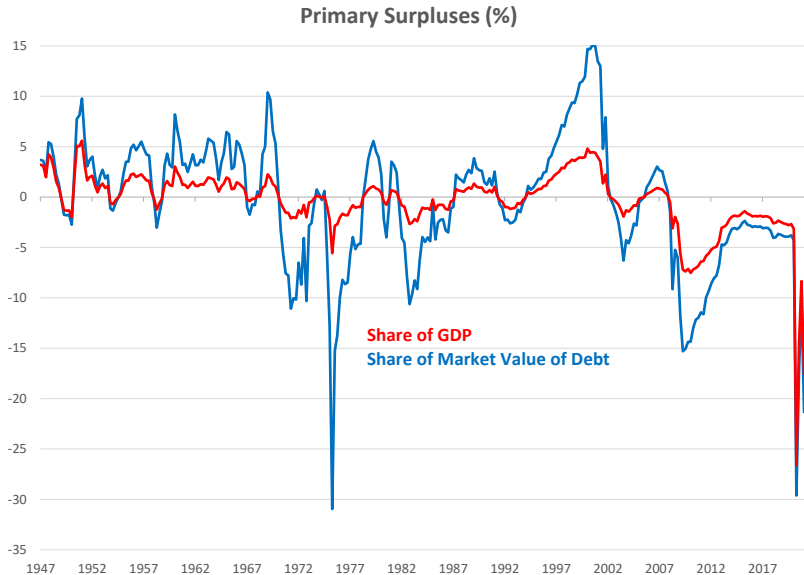
Fiscal Data

- ▶ We showed: conventional theory consistent with range of patterns of correlation
- ▶ Have the equilibrium condition

$$\frac{\sum_{j=0}^{\infty} Q_t^{(t+j)} B_{t-1}^{(t+j)}}{P_t} = E_t \sum_{j=0}^{\infty} q_{t,t+j} s_{t+j}$$

- ▶ Consider $ds_t < 0$ financed by $dB_t^{(t+j)} > 0$: possible adjustments
 - ▶ $P_t \uparrow$ (usual fiscal theory outcome)
 - ▶ $Q_t^{(t+j)} \downarrow \Rightarrow P_{t+j} \uparrow$
 - ▶ $s_{t+j} \uparrow \Rightarrow$ outcome depends on $dPV(s)$
 - ▶ $q_{t,t+j} \uparrow \Rightarrow$ outcome depends on $dPV(s)$
 - ▶ even possible $P_t \downarrow \Rightarrow$ all inflation in future
- ▶ Theoretical predictions—like data—hinge on how monetary & fiscal policies react

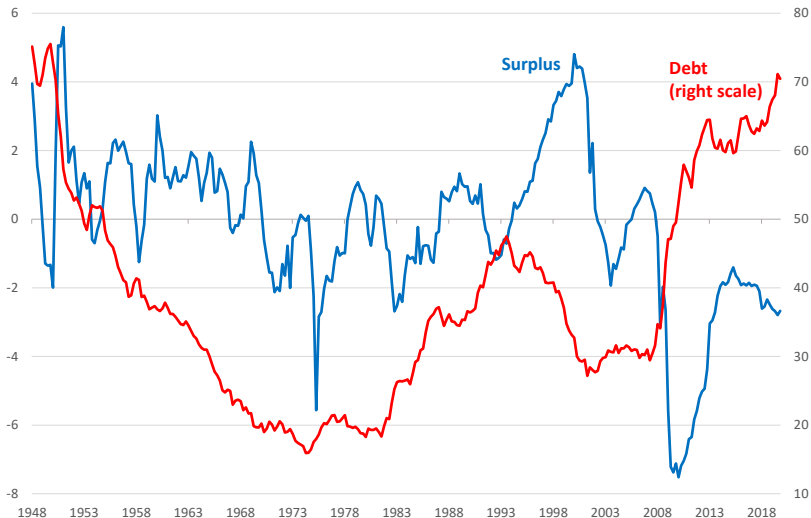
Primary Surpluses



What is a “fiscal impulse?”

Surplus & Debt

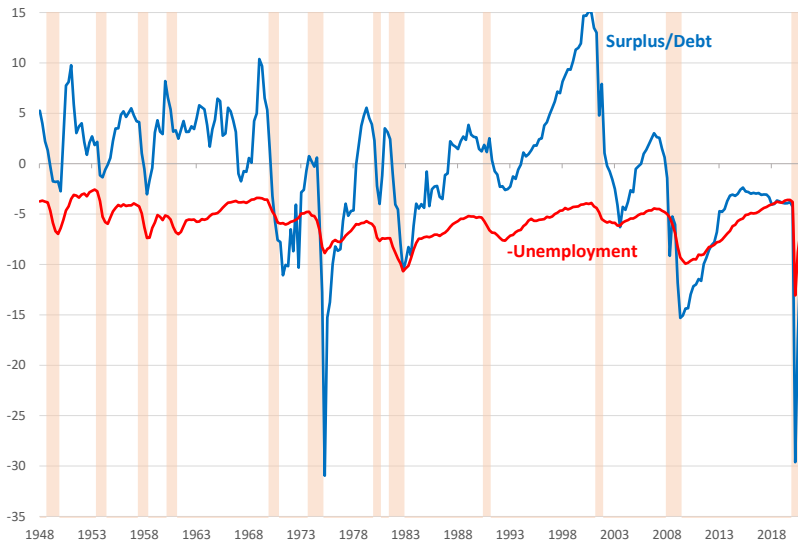
Primary Surplus & Debt
(% of GDP)



Surpluses help to retire debt

Surplus & Unemployment

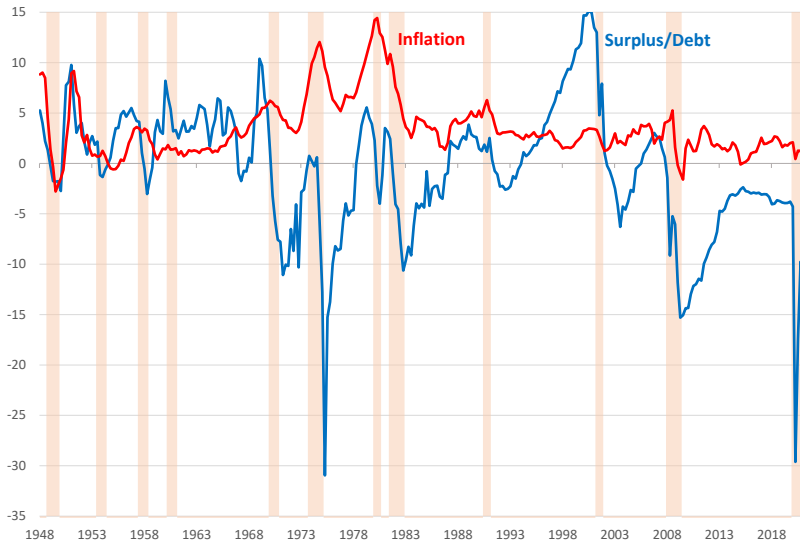
Primary Surplus/Debt & -Unemployment Rate



Surpluses move strongly with business cycle

Surplus & Inflation

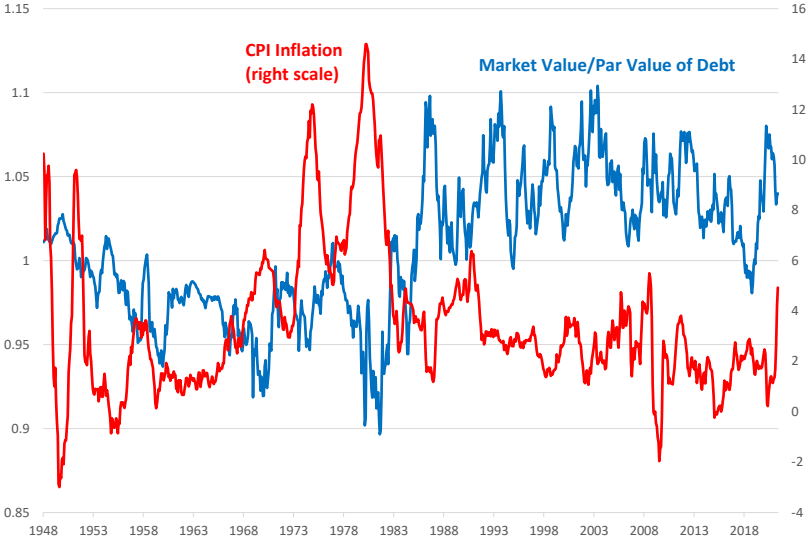
Primary Surplus/Debt & Inflation



Subtle dynamic correlation between surpluses & inflation

Bond Prices & Inflation

Bond Portfolio "Price" & Inflation



Bond prices generally reflect inflation trends

Going Beyond Pictures

- ▶ Cochrane's "Fiscal Roots of Inflation"
- ▶ A (largely) reduced-form exploration of dynamic correlations among components of the government's budget identity
- ▶ Some suggestive identification of "shocks"
- ▶ Obtains certain provocative results
- ▶ Don't need to buy his interpretations to find results useful
- ▶ Creative, full of ideas for further work

Budget Identity

- ▶ V_t is market value of nominal government liabilities

$$V_t \equiv M_t + \sum_{j=0}^{\infty} Q_t^{(t+1+j)} B_t^{(t+1+j)}$$

M_t : non-interest bearing money (“high-powered”)

B_t^{t+j} : zero-coupon bonds sold at t , due at $t + j$

- ▶ Define liability-GDP ratio

$$v_t \equiv \log \left(\frac{V_t}{P_t Y_t} \right)$$

- ▶ Nominal return on government portfolio

$$R_{t+1}^n \equiv \frac{M_t + \sum_{j=1}^{\infty} Q_{t+1}^{(t+j)} B_t^{(t+j)}}{M_t + \sum_{j=1}^{\infty} Q_t^{(t+j)} B_t^{(t+j)}}$$

- ▶ Further definitions

$$r_{t+1}^n \equiv \log(R_{t+1}^n), \quad \pi_t \equiv \log(P_t/P_{t-1}), \quad g_t \equiv \log(Y_t/Y_{t-1})$$

Budget Identity

- ▶ In levels

$$\sum_{j=0}^{\infty} Q_t^{(t+j)} B_{t-1}^{(t+j)} + M_{t-1} = P_t s p_t + \sum_{j=0}^{\infty} Q_t^{(t+1+j)} B_t^{(t+1+j)} + M_t$$

- ▶ Log-linearize around $\rho = e^{-(r-g)}$ with $r > g$

$$\rho v_{t+1} = v_t + r_{t+1}^n - \pi_{t+1} - g_{t+1} + s_{t+1}$$

$$v_t = \sum_{j=1}^{\infty} \rho^{j-1} s_{t+j} - \sum_{j=1}^{\infty} \rho^{j-1} (r_{t+j}^n - \pi_{t+j} - g_{t+j})$$

- ▶ Take innovations: $\Delta E_{t+1} \equiv E_{t+1} - E_t$ to yield surprise inflation identity

$$\begin{aligned} & \Delta E_{t+1} \pi_{t+1} - \Delta E_{t+1} (r_{t+1}^n - g_{t+1}) \\ &= - \sum_{j=0}^{\infty} \rho^j \Delta E_{t+1} s_{t+1+j} + \sum_{j=1}^{\infty} \rho^j \Delta E_{t+1} (r_{t+1+j}^n - \pi_{t+1+j} - g_{t+1+j}) \end{aligned}$$

(13)

Budget Identity Interpretations

► Interpretation

- $\Delta E_{t+1}\pi_{t+1}$: surprise inflation
- $\Delta E_{t+1}(r_{t+1}^n - g_{t+1})$: surprise return net of growth
- $\sum_{j=0}^{\infty} \rho^j \Delta E_{t+1}s_{t+1+j}$: surprise in PV real primary surpluses
- $\sum_{j=1}^{\infty} \rho^j \Delta E_{t+1}(r_{t+1+j}^n - \pi_{t+1+j} - g_{t+1+j})$: surprise in growth-adjusted real discount rate

$$\begin{aligned} & \Delta E_{t+1}\pi_{t+1} - \Delta E_{t+1}(r_{t+1}^n - g_{t+1}) \\ &= - \sum_{j=0}^{\infty} \rho^j \Delta E_{t+1}s_{t+1+j} + \sum_{j=1}^{\infty} \rho^j \Delta E_{t+1}(r_{t+1+j}^n - \pi_{t+1+j} - g_{t+1+j}) \end{aligned} \tag{13}$$

- What accounts for changes in surprise inflation?
 - current growth-adjusted returns
 - changes in path of surpluses
 - changes in real discount rates

Budget Identity Interpretations

- ▶ In the absence of identifying restrictions, an accounting exercise
- ▶ Akin to exercises in Leeper-Traum-Walker (2017) or Leeper-Zhou (2021) from structural models
 - ▶ in those, shocks are identified—given unambiguous structural interpretation
- ▶ Here we cannot make *causal* statements without further restrictions
- ▶ Cochrane employs some sign restrictions to identify a variety of “shocks”
 - ▶ but they are hard to map into a DSGE model
- ▶ Mostly, he just interprets results through lens of “fiscal theory of monetary policy”

Data

- ▶ Cochrane uses annual data on
 - ▶ market value of liabilities, V_t
 - ▶ nominal return on portfolio, R_{t+1}^m
 - ▶ inflation, π_t
 - ▶ growth rate of output, g_t
 - ▶ 3-month Treasury bill rate
 - ▶ 10-year constant maturity bond yield
- ▶ Uses linearized flow condition to back out $\{s_t\}$

$$\rho v_{t+1} = v_t + r_{t+1}^n - \pi_{t+1} - g_{t+1} + s_{t+1}$$

- ▶ Identity holds exactly, so a VAR with $\{v_t, r_t^n, \pi_t, g_t, s_t\}$ is stochastically singular

Maturity Structure

- ▶ Geometric structure: face value of maturity j debt declines at rate ω^j
- ▶ Then return on portfolio is

$$\begin{aligned}\Delta E_{t+1} r_{t+1}^n &= - \sum_{j=1}^{\infty} \omega^j \Delta E_{t+1} r_{t+1+j}^n \\ &= - \sum_{j=1}^{\infty} \omega^j \Delta E_{t+1} [(r_{t+1+j}^n - \pi_{t+1+j}) + \pi_{t+1+j}] \quad (14)\end{aligned}$$

- ▶ Lower bond prices correspond to higher bond expected nominal returns
- ▶ Bond return responses, $\Delta E_{t+1} r_{t+1}^n$ are large
 - ▶ mostly associated with expected inflation
 - ▶ not with expected real returns

Cochrane's Procedure

- ▶ Experiment with different orthogonalizations
- ▶ Not necessarily about “exogenous shocks” as in DSGE models
- ▶ Value of procedure
 - ▶ not about giving a “structural” interpretation to data
 - ▶ seeks interesting patterns of correlation
 - ▶ provides grist for future research
- ▶ I like this approach

“Inflation Shock”

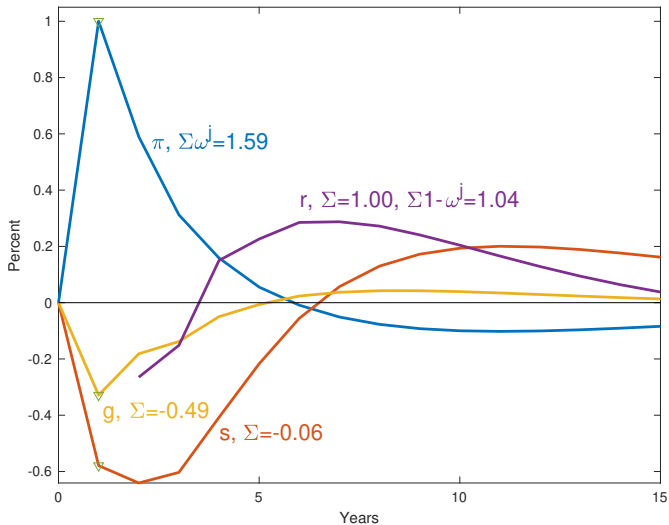
- ▶ Unexpected change in $\Delta E_1 \pi_1$
- ▶ Set $\varepsilon_1^\pi = 1$
- ▶ All variables move contemporaneously with ε_1^π
- ▶ For each variable z , regress

$$\varepsilon_{t+1}^z = b_{z,\pi} \varepsilon_{t+1}^\pi + \eta_{t+1}$$

- ▶ Start VAR at

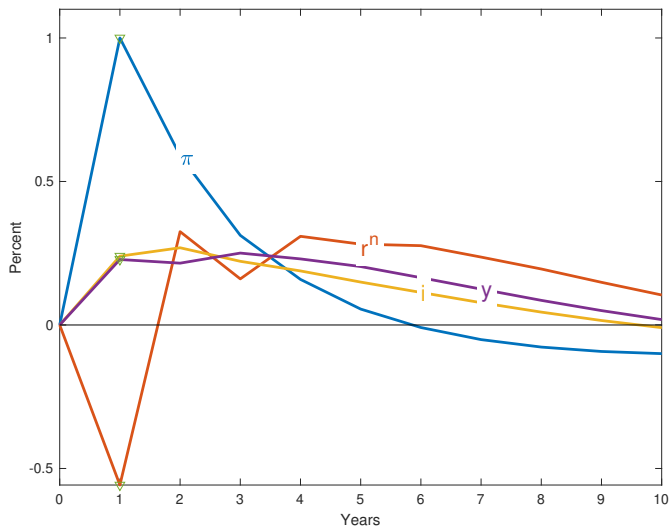
$$\varepsilon_1 = -[b_{r^n,\pi} \quad b_{g,\pi} \quad \varepsilon_1^\pi = 1 \quad b_{s,\pi} \quad \dots]'$$

“Inflation Shock”



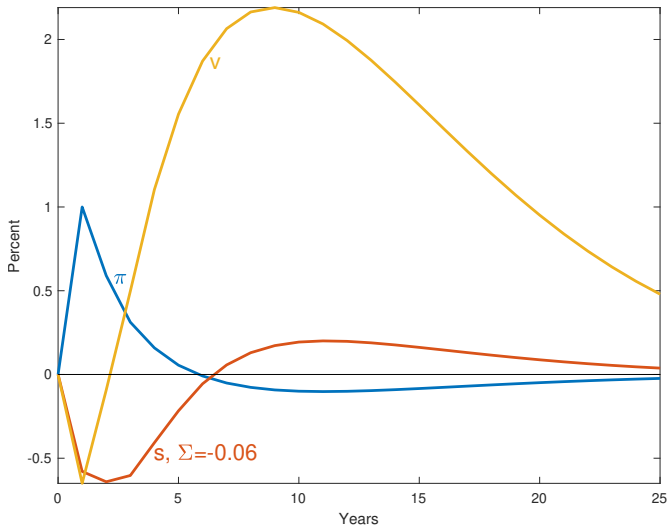
π : inflation, r : discount rate, g : growth rate, s : surplus

“Inflation Shock”



π : inflation, r^n : nominal return on bond portfolio, i : short nominal rate,
 y : long nominal rate

“Inflation Shock”



π : inflation, v : value of debt, s : surplus

“Inflation Shock”

$$\sum_{j=0}^{\infty} \omega^j \Delta E_1 \pi_{1+j} = - \sum_{j=0}^{\infty} \Delta E_1 s_{1+j} - \sum_{j=0}^{\infty} \Delta E_1 g_{1+j} + \sum_{j=1}^{\infty} (1 - \omega^j) \Delta E_1 r_{1+j}$$

	π	=	s	g	r
Inflation	1.59	=	-(-0.06)	-(-0.49)	+(1.04)
Recession	-2.36	=	-(-1.15)	-(-1.46)	+(-4.96)

$$\Delta E_1 \pi_1 - \Delta E_1 r_1^n = - \sum_{j=0}^{\infty} \Delta E_1 s_{1+j} - \sum_{j=0}^{\infty} \Delta E_1 g_{1+j} + \sum_{j=1}^{\infty} \Delta E_1 r_{1+j}$$

	π	r^n	=	s	g	r
Inflation	1.00	-(-0.56)	=	-(-0.06)	-(-0.49)	+(1.00)
Recession	-1.00	-(1.19)	=	-(-1.15)	-(-1.46)	+(-4.79)

$$\Delta E_1 r_1^n = - \sum_{j=1}^{\infty} \omega^j \Delta E_1 r_{1+j} - \sum_{j=1}^{\infty} \omega^j \Delta E_1 \pi_{1+j}$$

	r^n	=	r	π
Inflation	-0.56	=	-(-0.03)	-(0.59)
Recession	1.19	=	-(0.17)	-(-1.36)

π : inflation, s : surplus, g : growth rate, r : discount rate, r^n : nominal return on bond portfolio

Key Findings

- ▶ Unexpected inflation associated more strongly with rise in real discount rates than with surpluses
- ▶ Argues critical for understanding fiscal underpinnings of standard models
- ▶ Example: in 2008, why did inflation fall when deficits rose? Use (13)
 1. Perhaps $s_t < 0 \Rightarrow E_t s_{t+j} > 0$, with future s large enough to drive down π_t
 2. Real & nominal interest rates fell sharply, which plausibly raised value of unchanged s
- ▶ Consider $-\Delta E_{t+1}(r_{t+1}^n - g_{t+1})$
 - ▶ if $PV(s) \downarrow$, decline in long-term bond prices and $\Delta E_{t+1} r_{t+1}^n$ can lower real value of debt without higher inflation

“Recession Shock”

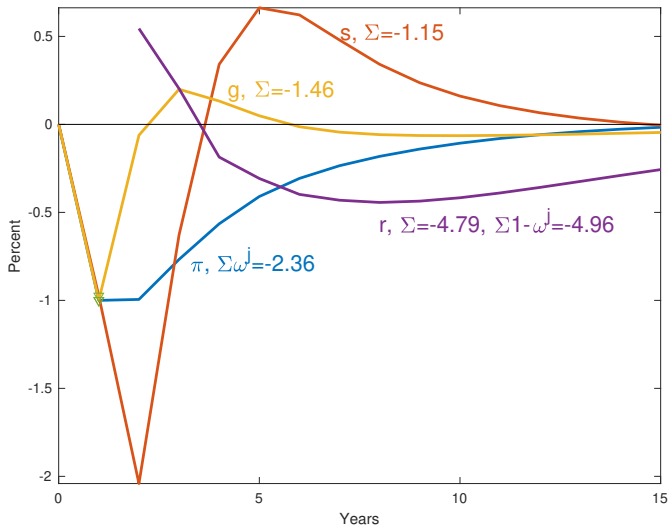
- ▶ Shock in which inflation & GDP go in same direction
- ▶ Set $\varepsilon_1^\pi = -1$ & $\varepsilon_1^g = -1$
- ▶ All variables move contemporaneously with these
- ▶ For each variable z , regress

$$\varepsilon_{t+1}^z = b_{z,\pi} \varepsilon_{t+1}^\pi + b_{z,g} \varepsilon_{t+1}^g + \eta_{t+1}$$

- ▶ Start VAR at

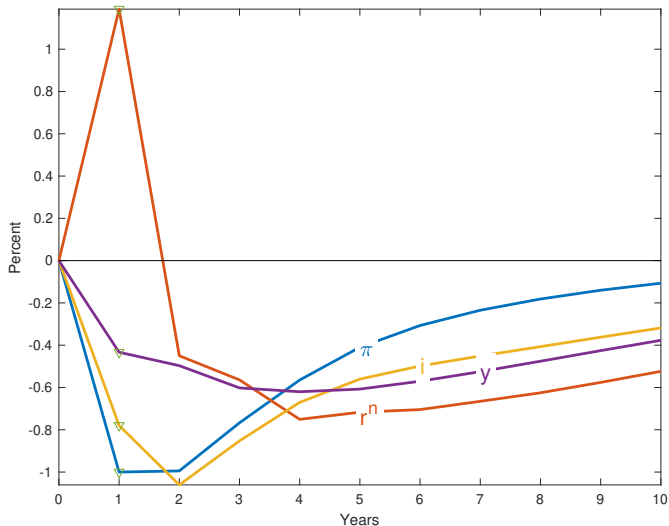
$$\varepsilon_1 = -[b_{r^n,\pi} + b_{r^n,g} \quad \varepsilon_1^g = 1 \quad \varepsilon_1^\pi = 1 \quad b_{s,\pi} + b_{s,g} \quad \dots]'$$

“Recession Shock”



π : inflation, r : discount rate, g : growth rate, s : surplus

“Recession Shock”



π : inflation, r^n : nominal return on bond portfolio, i : short nominal rate,
 y : long nominal rate

“Recession Shock”

$$\sum_{j=0}^{\infty} \omega^j \Delta E_1 \pi_{1+j} = - \sum_{j=0}^{\infty} \Delta E_1 s_{1+j} - \sum_{j=0}^{\infty} \Delta E_1 g_{1+j} + \sum_{j=1}^{\infty} (1 - \omega^j) \Delta E_1 r_{1+j}$$

	π	=	s	g	r
Inflation	1.59	=	-(-0.06)	-(-0.49)	+(1.04)
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$$\Delta E_1 \pi_1 - \Delta E_1 r_1^n = - \sum_{j=0}^{\infty} \Delta E_1 s_{1+j} - \sum_{j=0}^{\infty} \Delta E_1 g_{1+j} + \sum_{j=1}^{\infty} \Delta E_1 r_{1+j}$$

	π	r^n	=	s	g	r
Inflation	1.00	-(-0.56)	=	-(-0.06)	-(-0.49)	+(1.00)
Recession	-1.00	-(1.19)	=	-(-1.15)	-(-1.46)	+(-4.79)

$$\Delta E_1 r_1^n = - \sum_{j=1}^{\infty} \omega^j \Delta E_1 r_{1+j} - \sum_{j=1}^{\infty} \omega^j \Delta E_1 \pi_{1+j}$$

	r^n	=	r	π
Inflation	-0.56	=	-(-0.03)	-(0.59)
Recession	1.19	=	-(0.17)	-(-1.36)

π : inflation, s : surplus, g : growth rate, r : discount rate, r^n : nominal return on bond portfolio

Key Findings

- ▶ Disinflation in recessions driven by lower discount rate, along with lower short and long nominal rates
- ▶ Near-term deficits very large in recessions, but recover within a few years to become surpluses
- ▶ Persistent decline in inflation consistent with sharply lower discount rates that overcome inflation effects of deficits
- ▶ Suggests need to separately identify aggregate demand & supply

Wrap Up

- ▶ Cochrane considers other shocks
- ▶ Why is this approach useful?
 1. A way to ask interesting questions about the data: To what variables are surprise increases in inflation related and how are they related?
 2. It provokes reader to ask more structural questions: What underlying shock(s) generate the patterns associated with surprise inflation?
 3. It points to important & new variables to model: Real discount rates matter a lot
- ▶ We need more exploratory empirical work like this

Wrap Up

- ▶ Observation about discount rates: a crucial nexus of monetary-fiscal interactions
 - ▶ real interest rates are the linchpin of the MP transmission mechanism
 - ▶ surely, connection to discount rates is tight
 - ▶ discount rates affect $EPV(s)$ & value of debt
- ▶ Our macro models notoriously poor along asset-pricing dimensions
 - ▶ discount rates
 - ▶ time-varying term premia
 - ▶ exchange rates
- ▶ All critical components for understanding monetary & fiscal policies